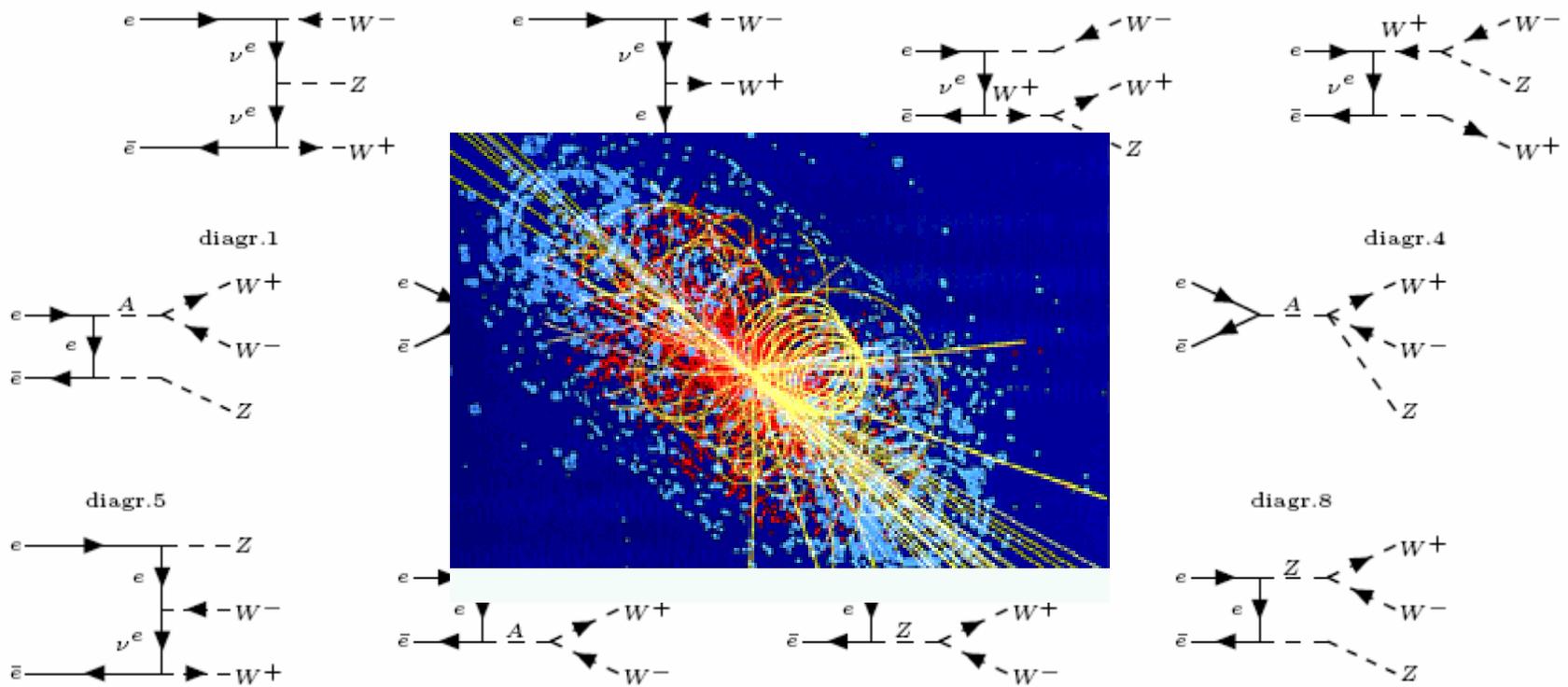


# A Particle Physics Tour with CompHEP

*Jeffrey D. Richman*



**April 26, 2006**

# Outline

- Introduction
- Getting, installing, and running CompHEP; references
- Using CompHEP; particle content in SM and SUSY; limitations of CompHEP; exclusive vs. inclusive processes; intermediate states
- “Observables” in particle physics: decay rates, cross sections,...
- Z-boson,  $t$ -quark, and Higgs decay in the SM
- Compton Scattering
- Muon decay and radiative corrections;  $b$ -quark decay
- $e^+ e^-$  scattering
- Structure functions
- $pp$  and  $p\bar{p}$  interactions: production of dijets,  $t$ -quarks,  $t\bar{t}H$
- Conclusions

# A Tour of Particle Physics with CompHEP

$Z \rightarrow 2 \text{ body}$	$t \rightarrow bW^+$	$\gamma + e^- \rightarrow \gamma + e^-$	$\mu^- \rightarrow e^- \bar{\nu}_e \nu_\mu$ $\mu^- \rightarrow e^- \bar{\nu}_e \nu_\mu \gamma$
$b \rightarrow ce^- \bar{\nu}_e$	$\bar{\nu}_e + e^- \rightarrow \bar{\nu}_\mu + \mu^-$	$e^+ e^- \rightarrow \gamma, Z \rightarrow \mu^+ \mu^-$ $e^+ e^- \rightarrow \gamma, Z \rightarrow b\bar{b}$	$e^+ + e^- \rightarrow W^+ + W^-$ $e^+ + e^- \rightarrow Z + Z$
$g + g \rightarrow g + g$	$g + g \rightarrow t + \bar{t}$ $q + \bar{q} \rightarrow t + \bar{t}$	$g + g \rightarrow t + \bar{t} + H$ $q + \bar{q} \rightarrow t + \bar{t} + H$ $g + g \rightarrow t + \bar{t} + b + \bar{b}$	$H \rightarrow q\bar{q},$ $\rightarrow W^+ W^-, ZZ$

Each one of these processes has a story to tell and could be investigated in much more depth...we will just scratch the surface.

# Getting CompHEP and Other Generators

- **CompHEP is a tool for calculating observables for particle processes, both scattering and decays**
  - ↗ developed at Moscow State University
  - ↗ powerful, simple and fast to use, but has significant limitations
  - ↗ a good tool for learning particle physics
  - ↗ CompHEP home page: <http://theory.sinp.msu.ru/comphep>
  - ↗ latest version is comphep-4.4.3 (25/05/2004)
  - ↗ documentation: hep-ph/9908288, hep-ph/0403113.
- **Comprehensive set of links to other Monte Carlo generators for hadron-collider physics**
  - ↗ <http://www.ippp.dur.ac.uk/montecarlo/BSM>
  - ↗ Les Houches Guidebook to Monte Carlo Generators for Hadron Physics (hep-ph/0403045)

Note: all figures in this talk were made by the author using CompHEP, FeynDraw, ROOT,...

# Installation for Linux

- Installation of CompHEP

- ↵ **download archive file (comphep-4.4.3.tgz) to your directory**

- ↵ **/home/richman/CompHEPSource**

- ↵ **tar xzvf comphep-4.4.3.tgz**

- ↵ **creates directory with name comphep-4.4.3**

- ↵ **cd comphep-4.4.3**

- ↵ **./configure**

- ⚡ **Note: the configure script looks for CERNLIB. You may need to change the CERNLIB environment variable to point to the appropriate directory. CERNLIB is needed only for SUSY models.**

- ↵ **make**

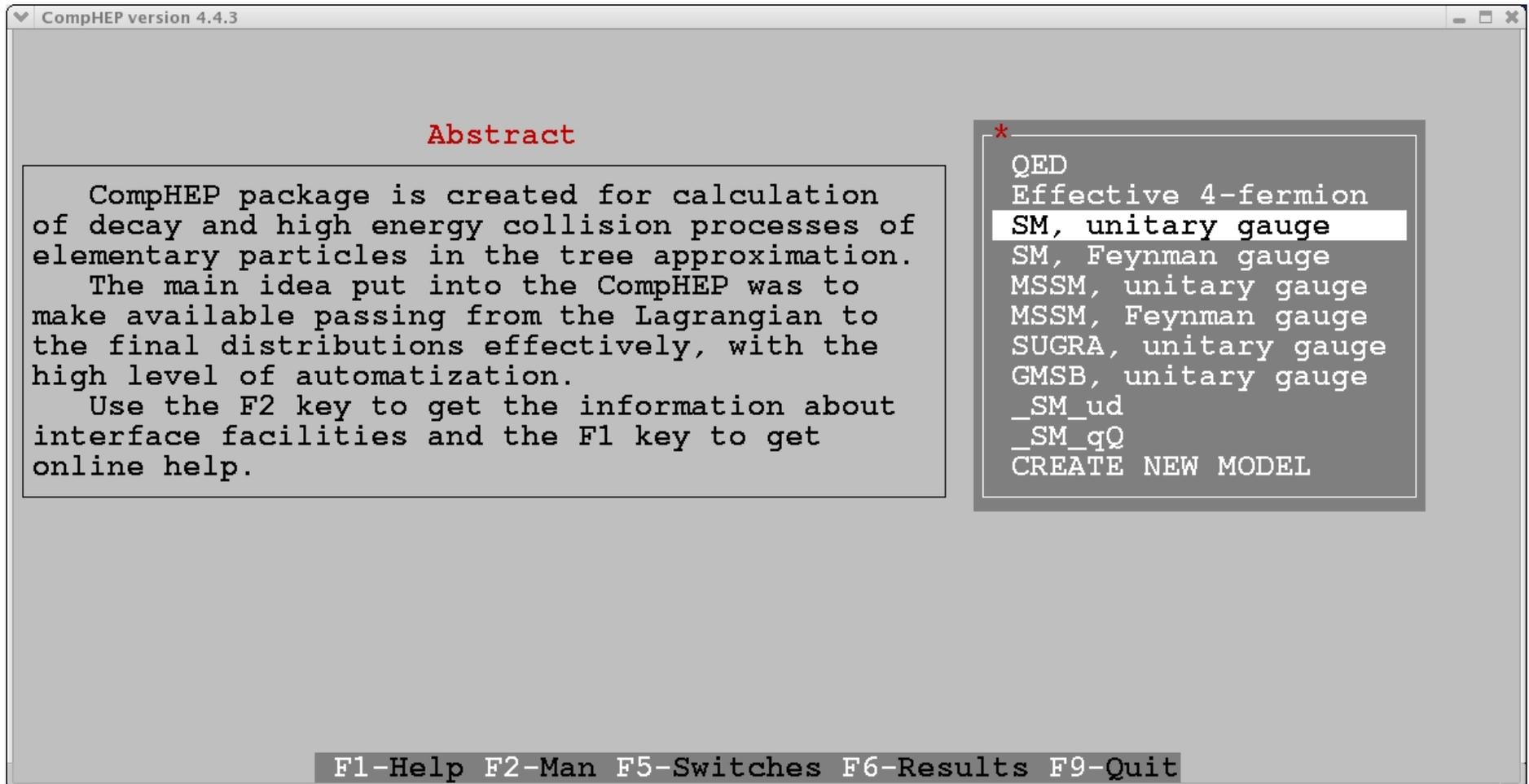
- ↵ **make setup WDIR=/home/richman/MyCompHEPWorkDir**

- Running CompHEP

- ↵ **cd ~/MyCompHEPWorkDir**

- ↵ **./comphep &**

# CompHEP Model Selection



CompHEP version 4.4.3

**Abstract**

CompHEP package is created for calculation of decay and high energy collision processes of elementary particles in the tree approximation.

The main idea put into the CompHEP was to make available passing from the Lagrangian to the final distributions effectively, with the high level of automatization.

Use the F2 key to get the information about interface facilities and the F1 key to get online help.

\*  
QED  
Effective 4-fermion  
**SM, unitary gauge**  
SM, Feynman gauge  
MSSM, unitary gauge  
MSSM, Feynman gauge  
SUGRA, unitary gauge  
GMSB, unitary gauge  
\_SM\_ud  
\_SM\_qQ  
CREATE NEW MODEL

F1-Help F2-Man F5-Switches F6-Results F9-Quit

# Particle Content of CompHEP: Standard Model

```
CompHEP version 4.4.3
Model: SM, unitary gauge

List of (anti)particles

G(G)      gluon      A(A)      photon    Z(Z)      Z boson
W+(W-)    W boson   ne(Ne)    neutrino  e(E)      electron
nm(Nm)    mu-neutrino m(M)      muon      nl(Nl)    tau-neutrino
l(L)      tau-lepton u(U)      u-quark   d(D)      d-quark
c(C)      c-quark   s(S)      s-quark   t(T)      t-quark
b(B)      b-quark   H(H)      Higgs

Enter decayed particle: H
Enter Final State: H -> Z,e,E
Exclude diagrams with
Keep diagrams with
```

*Can constrain possible intermediate-state particles; can be useful in reducing execution time when there are many possible Feynman diagrams and some have negligible amplitudes.*

# CompHEP Standard Model Parameters

Clr	Rest	Del	Size	Name	Value	> Comment <
				EE	0.31345	Elementary charge (alpha=1/127.9, on-shell, MZ
				GG	1.21358	Strong coupling constant (Z pnt, alp=0.1172pm0
				SW	0.48076	sin of the Weinberg angle (MZ point -> MW=79.9
				s12	0.2229	Parameter of C-K-M matrix (PDG2002)
				s23	0.0412	Parameter of C-K-M matrix (PDG2002)
				s13	0.0036	Parameter of C-K-M matrix (PDG2002)
				MZ	91.1876	mass of Z boson
				wZ	2.43631	width of Z boson
				wW	2.02798	width of W boson
				Mm	0.10566	mass of muon
				Mtau	1.77699	mass of tau-lepton
				Mc	1.65	mass of c-quark
				Ms	0.117	mass of s-quark
				Mtop	174.3	mass of t-quark
				wtop	1.54688	width of t-quark
				Mb	4.85	mass of b-quark
				MH	115	mass of Higgs
				wH	0.0061744	width of Higgs

F1 F2 Top Bottom GoTo Find Zoom ErrMes

*Also a separate menu of constraints, such as CKM unitarity relations.*

# Particle Content of CompHEP: Minimal SUSY

CompHEP version 4.4.3  
**Model:** MSSM, unitary gauge

List of (anti)particles

A(A)	photon	Z(Z)	Z boson	W+(W-)	W boson
G(G)	gluon	e(E)	electron	m(M)	muon
ne(Ne)	e-neutrino	nm(Nm)	mu-neutrino	nl(Nl)	tau-neutrino
l(L)	tau-lepton	s(S)	s-quark	c(C)	c-quark
u(U)	u-quark	d(D)	d-quark	t(T)	t-quark
b(B)	b-quark	h(h)	Light Higgs	H(H)	Heavy higgs
H3(H3)	CP-odd Higgs	H+(H-)	Charged Higgs	~l+(~l-)	chargino 1
~2+(~2-)	chargino 2	~o1(~o1)	neutralino 1	~o2(~o2)	neutralino 2
~o3(~o3)	neutralino 3	~o4(~o4)	neutralino 4	~G(~G)	gluino
~eL(~eL)	selectron L	~eR(~eR)	selectron R	~mL(~mL)	smuon L
~mR(~mR)	smuon R	~l1(~l1)	stau 1	~l2(~l2)	stau 2
~ne(~ne)	e-sneutrino	~nm(~nm)	mu-sneutrino	~nl(~nl)	tau-sneutrino

PgDn

Enter decayed particle: H  
 Enter Final State: H -> 2\*x  
 Exclude diagrams with  
 Keep diagrams with

CompHEP version 4.4.3  
**Model:** MSSM, unitary gauge

List of (anti)particles

u(U)	u-quark	d(D)	d-quark	t(T)	t-quark
b(B)	b-quark	h(h)	Light Higgs	H(H)	Heavy higgs
H3(H3)	CP-odd Higgs	H+(H-)	Charged Higgs	~l+(~l-)	chargino 1
~2+(~2-)	chargino 2	~o1(~o1)	neutralino 1	~o2(~o2)	neutralino 2
~o3(~o3)	neutralino 3	~o4(~o4)	neutralino 4	~G(~G)	gluino
~eL(~eL)	selectron L	~eR(~eR)	selectron R	~mL(~mL)	smuon L
~mR(~mR)	smuon R	~l1(~l1)	stau 1	~l2(~l2)	stau 2
~ne(~ne)	e-sneutrino	~nm(~nm)	mu-sneutrino	~nl(~nl)	tau-sneutrino
~uL(~uL)	u-squark L	~uR(~uR)	u-squark R	~cL(~cL)	c-squark L
~cR(~cR)	c-squark R	~t1(~t1)	t-squark 1	~t2(~t2)	t-squark 2
~dR(~dR)	d-squark R	~dL(~dL)	d-squark L	~sL(~sL)	s-squark L
~sR(~sR)	s-squark R	~b1(~b1)	b-squark 1	~b2(~b2)	b-squark 2

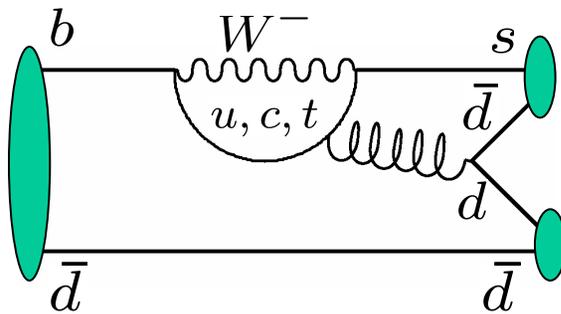
PgUp

# Some useful features of CompHEP

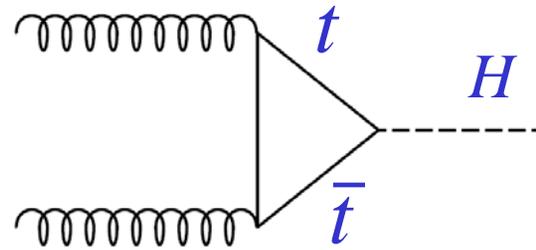
- You can restrict/specify the particles that enter in the intermediate state
- CompHEP provides a menu of structure functions, including the CTEQ6 series, which can be used to help compute  $pp$  scattering processes.
- You can apply cuts before computing cross sections; sometimes this is necessary to remove divergences.
- You can write out “events.”
- CompHEP can perform calculations in various SUSY models; this requires CERNLIB.

# CompHEP Limitations

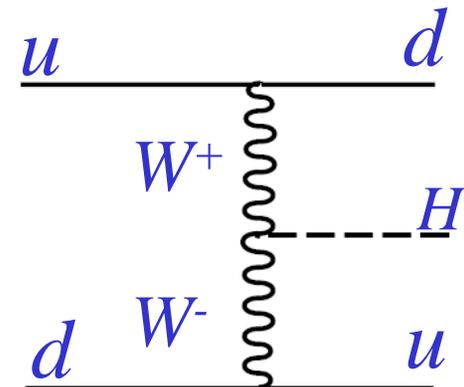
- No hadronic bound states (mesons, baryons) and no hadronization of quarks and gluons into jets
- No loop/box diagrams
- All processes are averaged over allowed initial-state spin polarizations and summed over final-state polarizations.
- No neutrino oscillations
- CompHEP can be used to compute quasi-inclusive processes (e.g.,  $H \rightarrow 2^*x$ ), but it is awkward to perform truly inclusive calculations.



*No, No*



*No*



*Yes*

# Procedure for computing results

1. Specify decay or scattering process
2. View Diagrams; can write Latex code; can Delete selected diagrams; Exit (escape key)
3. Square Diagrams (can View and escape)
4. Symbolic calculation
5. Write results
6. C code
7. C-Compiler (hit return in separate window after complete)
8. Go to new window for numerical calculations
9. Select subprocess if applicable
10. Define cuts if desired
11. Vegas (or Simpson if applicable)
12. Set distributions and ranges if desired
13. Integrate ( $X^2 < 1$  for numerically consistent results)
14. View distributions
15. Generate events if desired

# “Observables” in CompHEP

- **CompHEP allows us to compute the main “observables” that can be predicted by theories of particle physics.**
  - ↪ Decay rates of particles (and lifetimes)
  - ↪ Scattering cross sections
  - ↪ Differential distributions for both scattering and decays processes
  - ↪ Decay rates and asymmetries as a function of a parameter
- **Note that *none* of these quantities is directly measured with a detector!**
  - ↪ charged particles → ionization in detector → voltages/charges
  - ↪ neutral particles → generate EM or hadronic showers...
  - ↪ energy loss, multiple scattering, Cerenkov radiation, radiation damage,...
  - ↪ Particle interactions with the detector or not simulated by CompHEP, but they form the fundamental basis of our measurements!

# Observables: Decay Rates

The total decay rate ( $\Gamma$ ) of a particle measures

- the strength, range of the interactions governing the decay processes
- the number of accessible final states that the particle can decay into
- for a given final state, the possible effects of interference among different amplitudes

Exponential decay law: number of surviving particles

$$N(t) = N_0 e^{-t/\tau} = N_0 e^{-\Gamma t}$$

$$\Gamma = \sum_{f=1}^m \Gamma_f$$

*Decays/sec summed over all distinguishable final states  $f$*

Normally write  $\Gamma$  in energy units:

$$\Gamma \left( \frac{\text{decays}}{\text{sec}} \right) \rightarrow (\hbar\Gamma) (\text{Energy})$$

$$\tau = \frac{\hbar}{\Gamma} \cong \frac{65.8 \text{ MeV} \cdot 10^{-23} \text{ s}}{\Gamma}$$

# Observables: Decay Rates

Branching fractions ( $B_f$ )

$$1 = \sum_{f=1}^m \frac{\Gamma_f}{\Gamma} = \sum_{f=1}^m B_f$$

Each mode  $i$  corresponds to a distinguishable set of final-state particles and is called a “subprocess” in CompHEP.

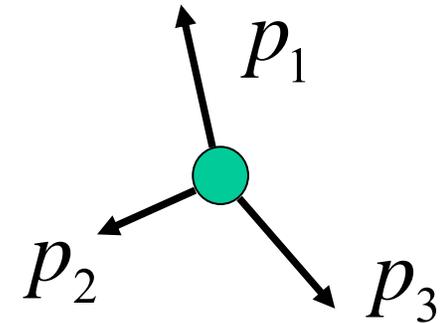
Differential decay rate for mode  $i$  (in diff. region of phase space)

$$d\Gamma_f = \frac{(2\pi)^4}{2M} |\mathcal{M}_f|^2 d\Phi_n(P; p_1, \dots, p_n)$$

sum of amplitudes for specified final state

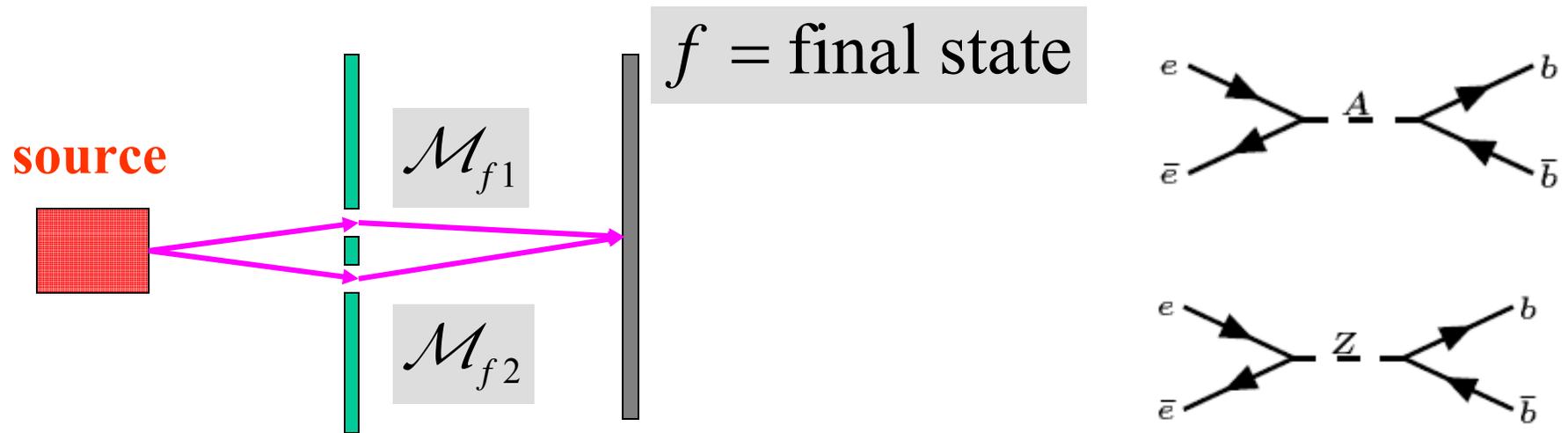
$$\mathcal{M}_f = \mathcal{M}_{f1} + \mathcal{M}_{f2} + \dots$$

phase space factor: integrate it over kinematic configurations consistent with  $(E, \mathbf{p})$  conservation



$$d\Phi_n(P; p_1, \dots, p_n) = \delta^4(P - \sum_{i=1}^n p_i) \prod_{i=1}^n \frac{d^3 p_i}{(2\pi)^3 (2E_i)}$$

# Initial states, intermediate states, and final states



- Sum the rate over final states (they are distinguishable)
- Sum the amplitudes over intermediate states (they are not distinguishable)
- Average the resulting rate over possible initial states
- Interference pattern allows us to infer that there is more than one intermediate state!

# CompHEP: $Z \rightarrow 2^*x$ subprocesses

Model: SM, unitary gauge

Process:  $Z \rightarrow 2^*x$

Feynman diagrams

13 diagrams in 13 subprocesses are constructed.  
0 diagrams are deleted.

NN	Subprocess	Del	Rest
*			
1	$Z \rightarrow b, B$	0	1
2	$Z \rightarrow t, T$	0	1
3	$Z \rightarrow s, S$	0	1
4	$Z \rightarrow c, C$	0	1
5	$Z \rightarrow d, D$	0	1
6	$Z \rightarrow u, U$	0	1
7	$Z \rightarrow l, L$	0	1
8	$Z \rightarrow n1, N1$	0	1
9	$Z \rightarrow m, M$	0	1
10	$Z \rightarrow nm, Nm$	0	1
11	$Z \rightarrow e, E$	0	1

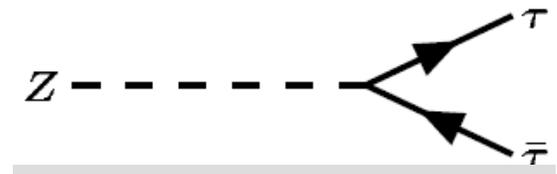
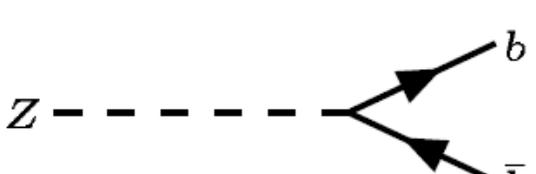
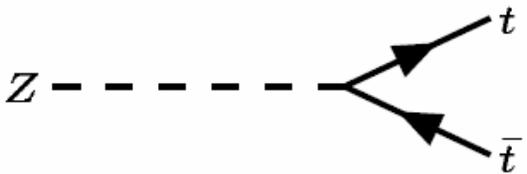
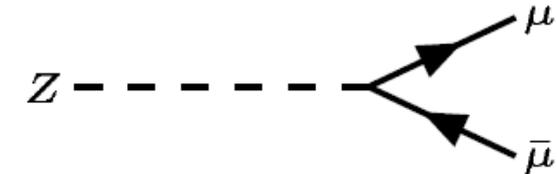
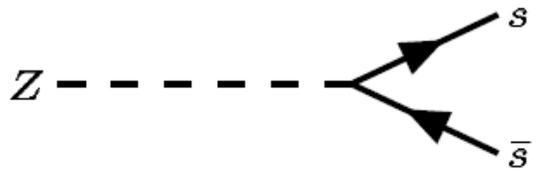
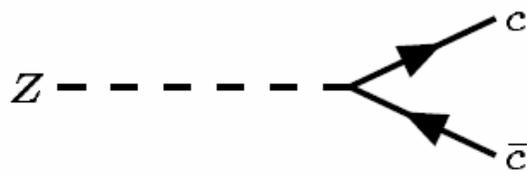
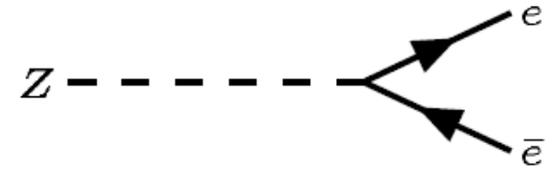
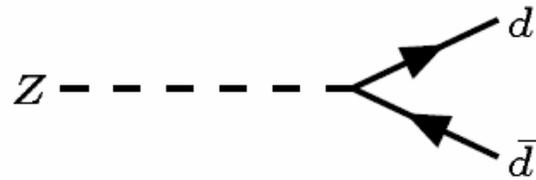
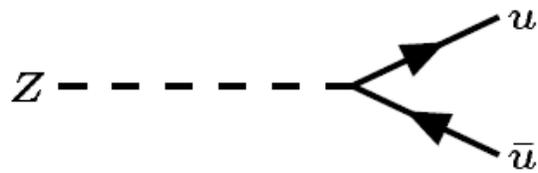
PgDn

F1-Help F2-Man F3-Model F5-Switches F6-Results F7-Del F8-UnDel F9-Quit

Each subprocess corresponds to a distinguishable final state; we need to add the rates for the subprocesses, not the amplitudes.

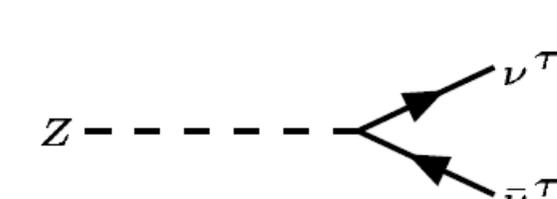
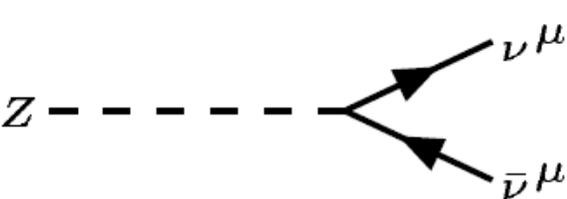
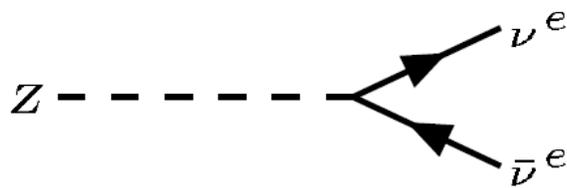
# CompHEP Diagrams for $Z \rightarrow 2^*x$

These diagrams are distinct subprocesses: no interference.



*Note: kinematically forbidden diagram.*

*in CompHEP menus, tau is l*



*Left out  $Z \rightarrow W^+W^-$  diagram, also kinematically forbidden.*

# Examples

## *CompHEP results for $Z \rightarrow 2^*x$*

```
Total width : 2.436309E+00 GeV
Modes and fractions :
b B - 15%          d D - 15%          s S - 15%
nl Nl - 6.9%      u U - 12%          c C - 12%
e E - 3.5%        nm Nm - 6.9%      ne Ne - 6.9%
t T - 0%          m M - 3.5%        l L - 3.4%
W+ W- - 0%
```

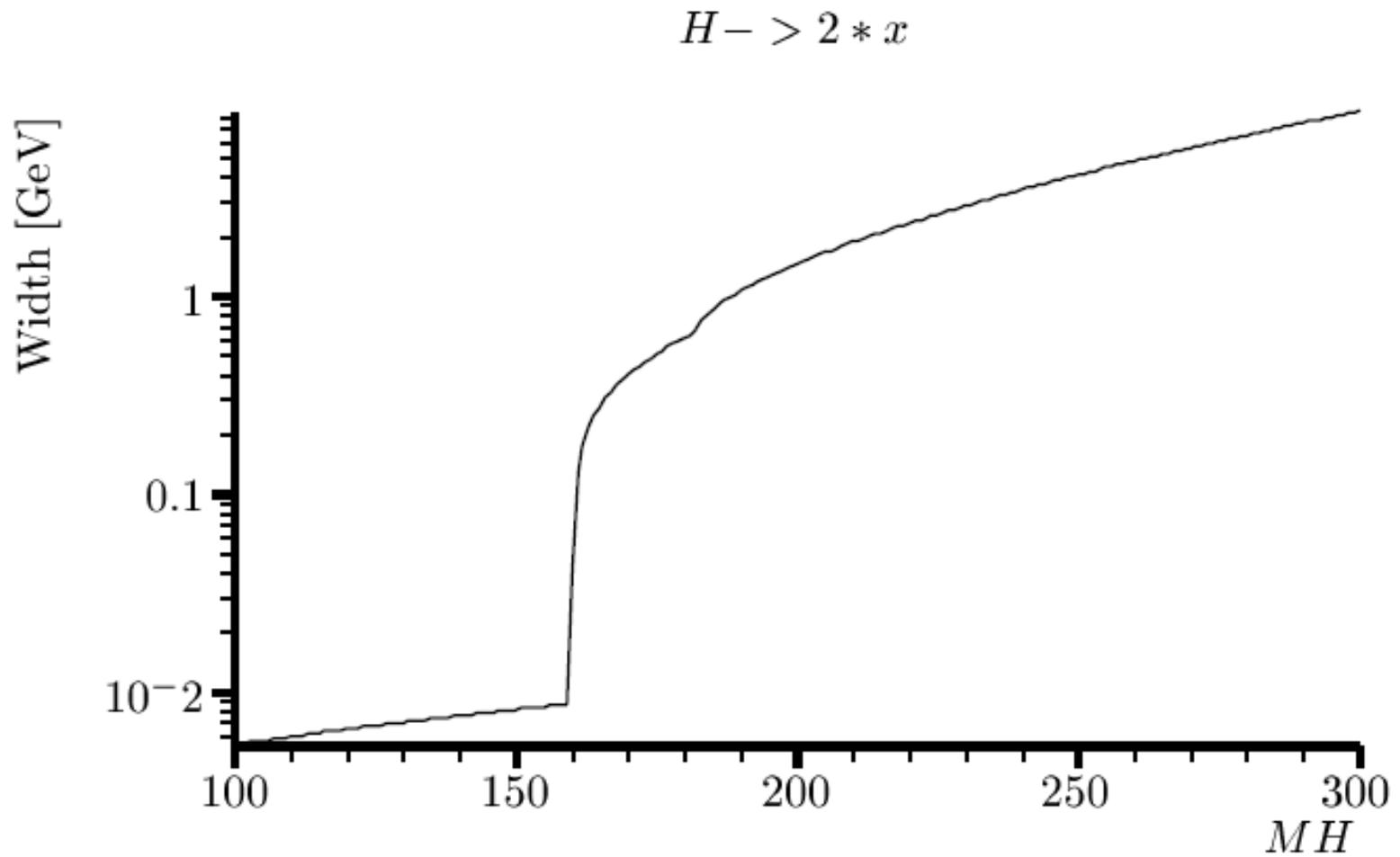
## *CompHEP results for $t \rightarrow 2^*x$*

```
Total width : 1.546882E+00 GeV
Modes and fractions :
W+ d - 0.0032%    W+ b - 1E+02%          W+ s - 0.17%
```

$$\tau_t \simeq \frac{65.8 \text{ MeV} \times 10^{-23} \text{ s}}{1.55 \text{ GeV}} \simeq 4.4 \times 10^{-25} \text{ s}$$

The top quark decays before it has time to form a hadronic bound state!

# SM Higgs Decay $H \rightarrow 2 * x$

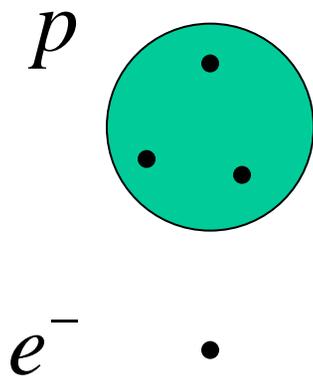


# Observables: Scattering Cross Sections

The scattering cross section ( $\sigma$ ) of two particles measures

- the strength and range of the interactions governing the scattering processes
- the number of accessible final states that the particles can scatter into
- for a given final state, the possible effects of interference among different amplitudes

*imagine a particle coming directly at you...*



If interaction is short range, and particle has finite extent, then the cross section roughly corresponds to the geometric area of the particle.

If interaction is long range, and/or particle has no finite extent, the cross section does not correspond to a geometrical area.

$$1 \text{ barn} = 10^{-24} \text{ cm}^2$$

# $p\bar{p}$ and $pp$ cross sections

## $pp$ cross sections (LHC)

$$\sigma_{tot} \approx 100 \text{ mb}$$

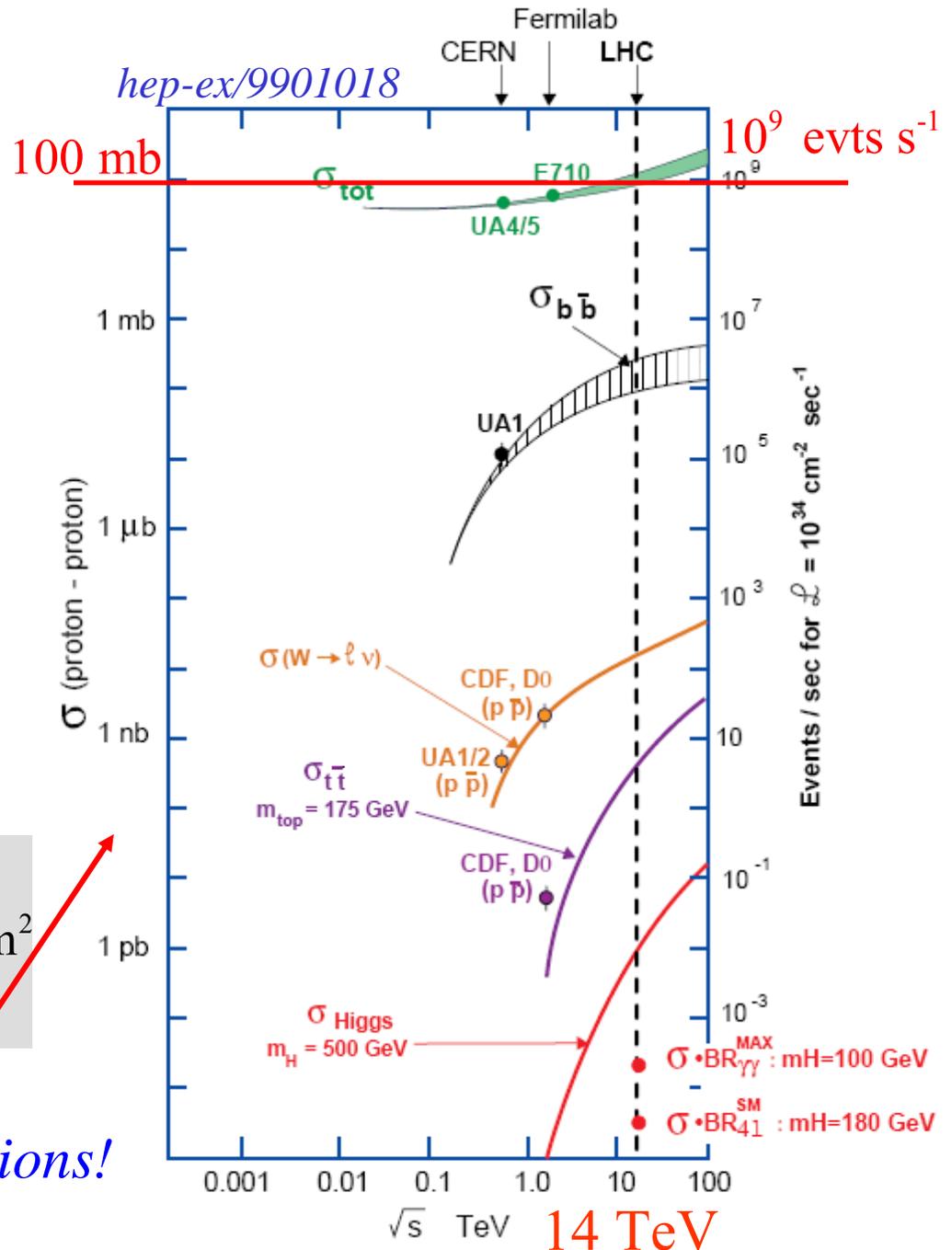
$$\sigma_{inelastic} \approx 80 \text{ mb}$$

$$\sigma_{elastic} \approx 20 \text{ mb}$$

Geometric cross section (very naïve)

$$\begin{aligned} \sigma(NN) &\approx \pi r_{nucleus}^2 \approx \pi(1.2 \text{ fm } A^{1/3})^2 \\ &\approx \pi(1.2 \times 10^{-13} \text{ cm})^2 \cdot A^{2/3} \cdot 10^{24} \text{ barn / cm}^2 \\ &\approx 30 \text{ mb } (pp) \end{aligned}$$

*Huge range of cross sections!*



# Observables: Scattering Cross Sections

$$N(t) = N_0 e^{-x/\lambda} \quad \lambda = \frac{1}{n\sigma} \quad \left. \vphantom{N(t)} \right\} \begin{array}{l} \text{scattering from a fixed target with} \\ n = \# \text{scattering objects/volume} \\ \lambda_{\text{nucl int}}^{-1}(\text{Fe}) = n\sigma \approx (25 \text{ cm})^{-1} \end{array}$$

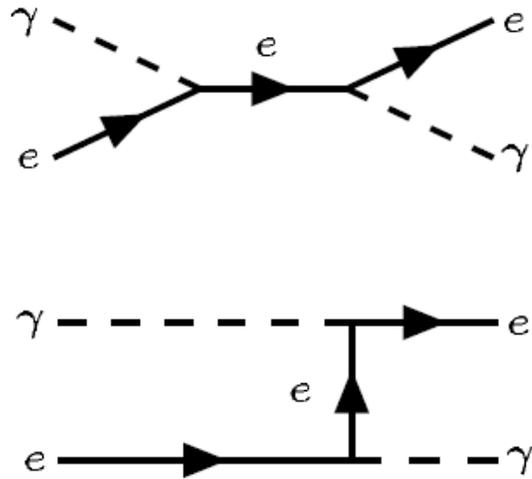
$$N_{\text{interactions}} = \left( \int dt L(t) \right) \cdot \sigma \quad \left. \vphantom{N_{\text{interactions}}} \right\} \begin{array}{l} \text{colliding-beam experiment} \\ L(t) = \text{instantaneous luminosity} \\ (\text{cm}^{-2}\text{s}^{-1}) \quad L(t) = \frac{N_1 N_2 n_B f}{A} \end{array}$$

$$d\sigma_f = \frac{(2\pi)^4}{4\sqrt{(p_1 \cdot p_2)^2 - m_1^2 m_2^2}} |\mathcal{M}_f|^2 d\Phi_n(p_1 + p_2; p_3, \dots, p_{n+2})$$

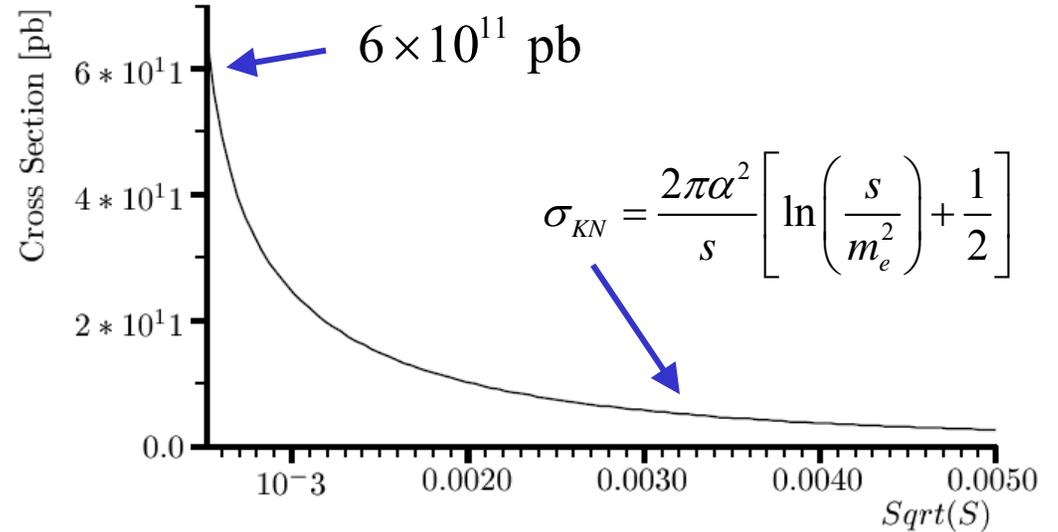
$$\mathcal{M}_f = \mathcal{M}_{f,1} + \mathcal{M}_{f,2} + \dots$$

$$d\Phi_n(P; p_1, \dots, p_n) = \delta^4(P - \sum_{i=1}^n p_i) \prod_{i=1}^n \frac{d^3 p_i}{(2\pi)^3 (2E_i)}$$

# $\gamma + e^- \rightarrow \gamma + e^-$ (Compton Scattering)



$A, e^- \rightarrow A, e$



$$\sigma(\gamma + e^- \rightarrow \gamma + e^-) = \frac{\pi\alpha^2(1-v)}{m_e^2 v^3} \times \left[ \frac{4v}{1+v} + (v^2 + 2v - 2) \ln\left(\frac{1+v}{1-v}\right) - \frac{2v^3(1+2v)}{(1+v)^2} \right]$$

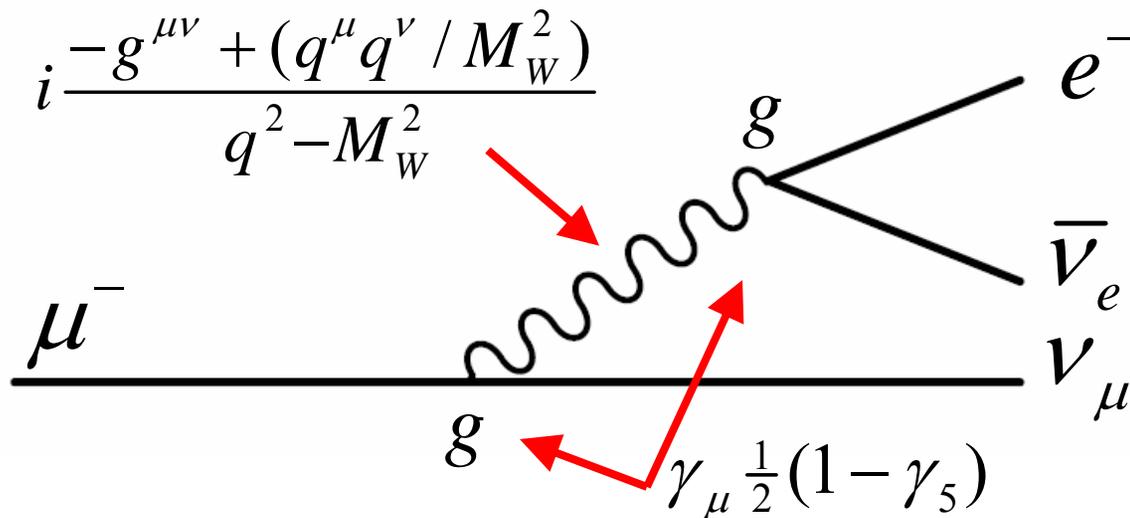
$$v = \frac{s - m_e^2}{s + m_e^2}$$

*Thomson scattering*

$$v \rightarrow 0 \Rightarrow \sigma \rightarrow \frac{8\pi\alpha^2}{3m_e^2} = \frac{8\pi\left(\frac{1}{137}\right)^2 (1973 \times 10^{-6} \text{ MeV} \cdot 10^{-8} \text{ cm})^2}{3(0.511 \text{ MeV})^2} \simeq 0.67 \times 10^{-24} \text{ cm}^2$$

# Muon decay: a prototype low-energy weak decay

$W$ -mediated  $b$ -quark transitions have several key features in common with muon decay.



$$q^2 \leq m_\mu^2 \ll M_W^2$$

Very strong dependence of decay rate on mass!

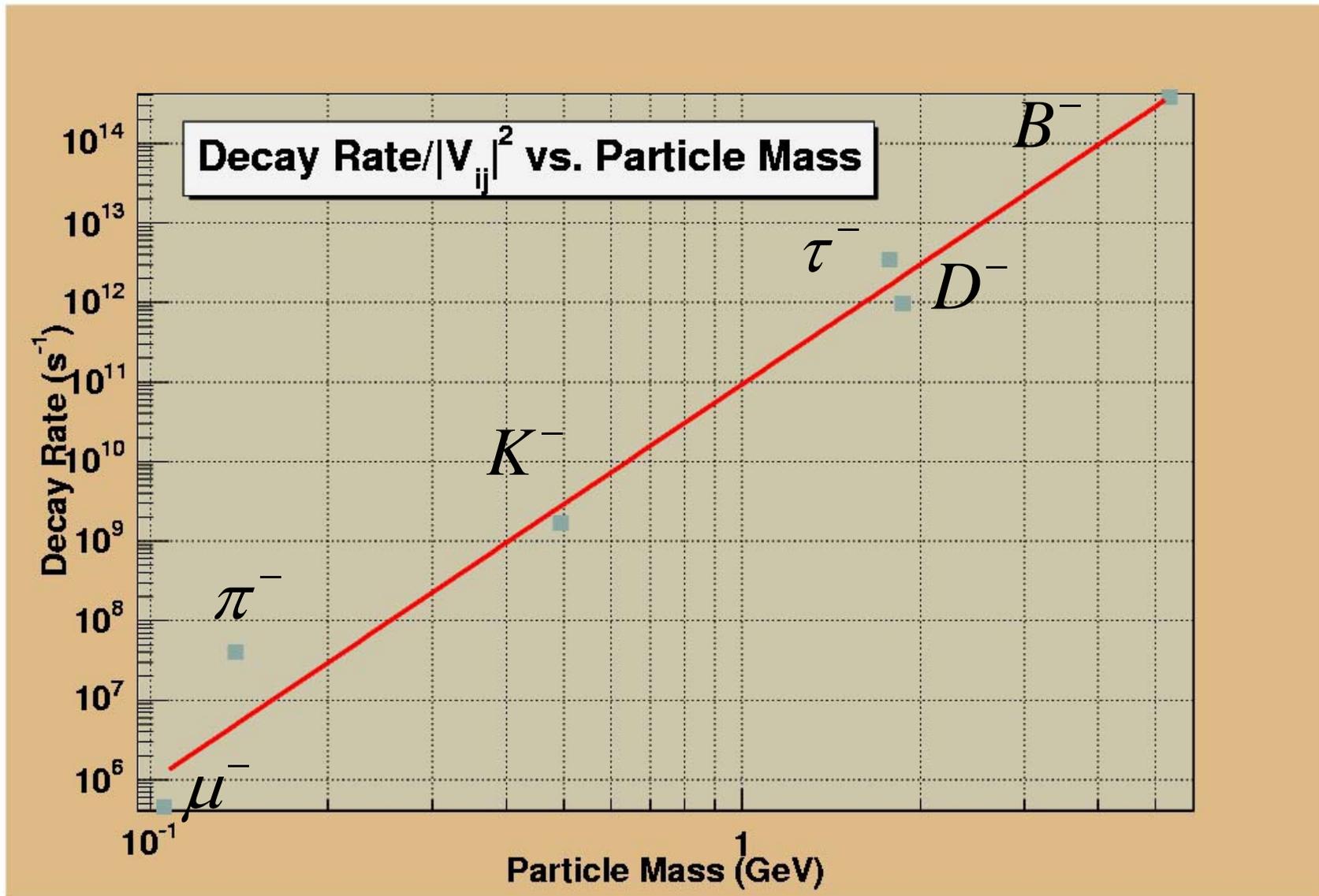
$$\Gamma = \frac{G_F^2 m_\mu^5}{192\pi^3} \cdot (1 - 8x + 8x^3 - x^4 - 12x^2 \ln x)$$

(ignoring QED radiative corrections)

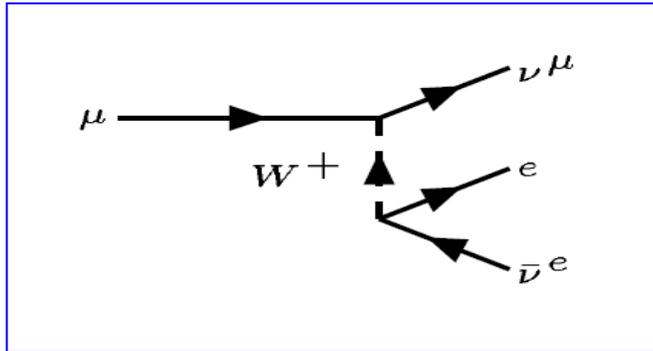
$$\frac{G_F}{\sqrt{2}} \equiv \frac{g^2}{8M_W^2}$$

$$x \equiv \frac{m_e^2}{m_\mu^2}$$

# Mass dependence of weak decay rates (correcting for CKM elements)

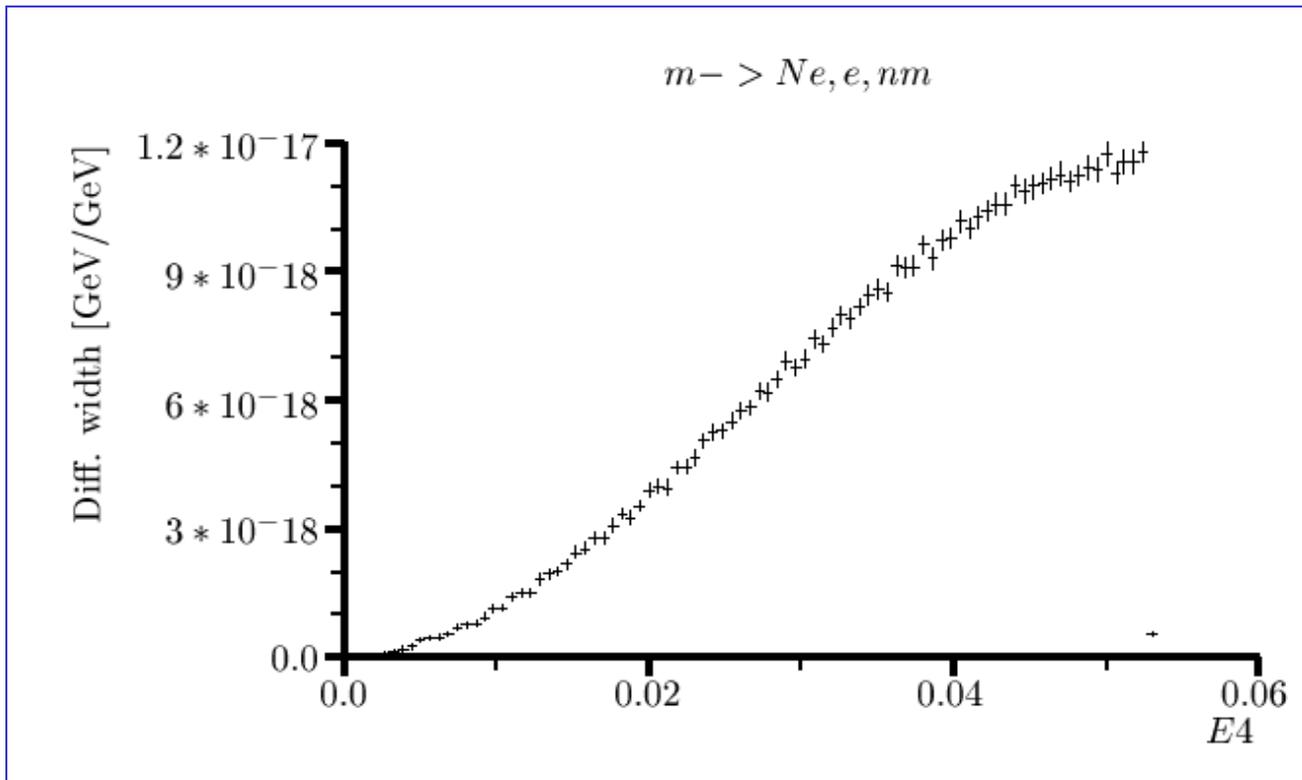


# $\mu$ Decay Rate and Distributions



$$\Gamma(\mu^- \rightarrow e^- \bar{\nu}_\mu \bar{\nu}_e) = (3.05 \times 10^{-19}) \text{ GeV}$$

$$\Rightarrow \tau = \frac{\hbar}{\Gamma_{tot}} \cong 2.16 \times 10^{-6} \text{ s}$$

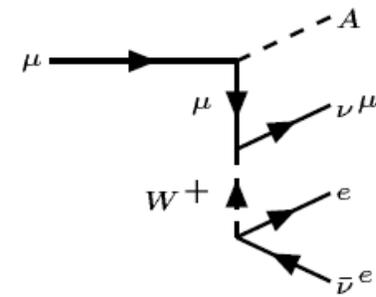
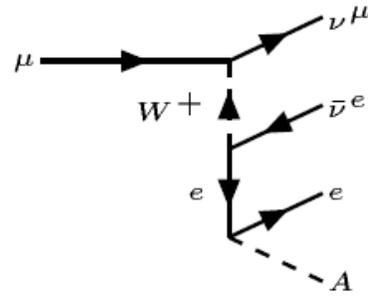
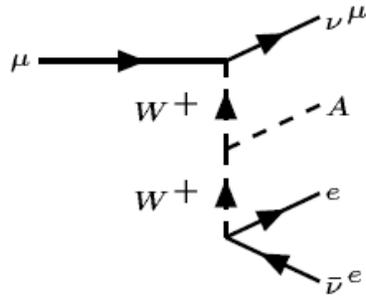


Electron energy spectrum  
 $\rightarrow$  coupling is  
 V, A comb.  
 (excludes T,S,P)

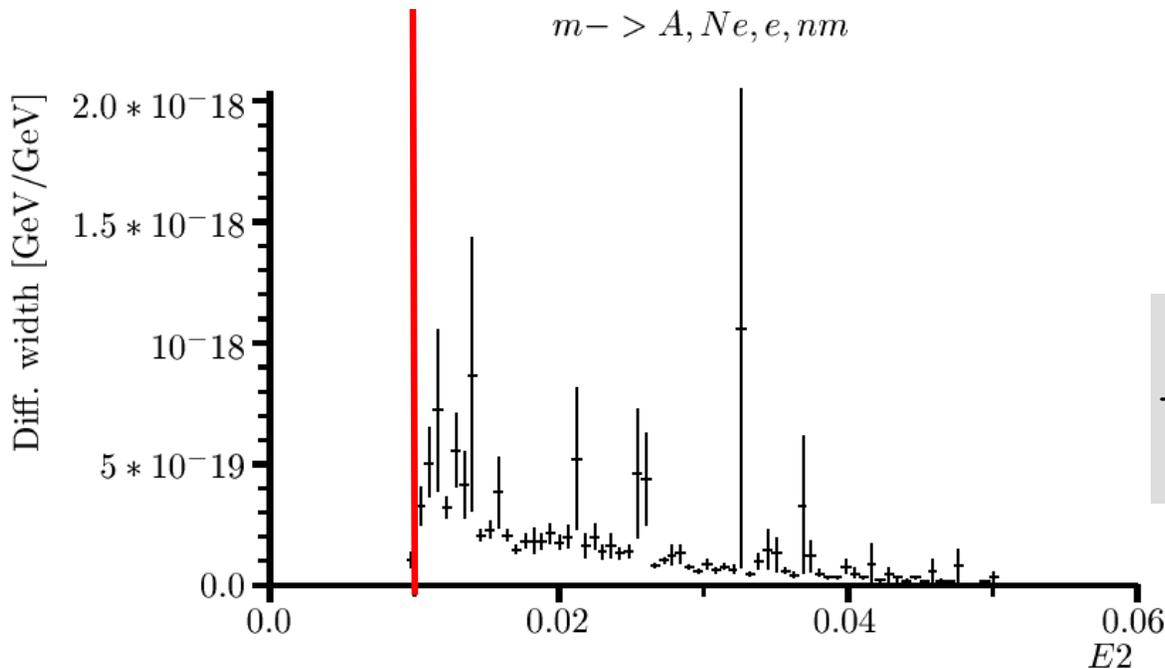
$$\frac{d\Gamma}{dx} = \frac{G_F^2 m_\mu^5}{96\pi^3} x^2 (3-2x)$$

$$x \equiv \frac{2E_e}{m_\mu}$$

# $\mu$ Decay with Radiative Corrections



$\gamma$  energy spectrum:  $E_\gamma > 10$  MeV



$$\Gamma(\mu^- \rightarrow e^- \nu_\mu \bar{\nu}_e \gamma)$$

$$= (5.0 \times 10^{-21}) \text{ GeV}$$

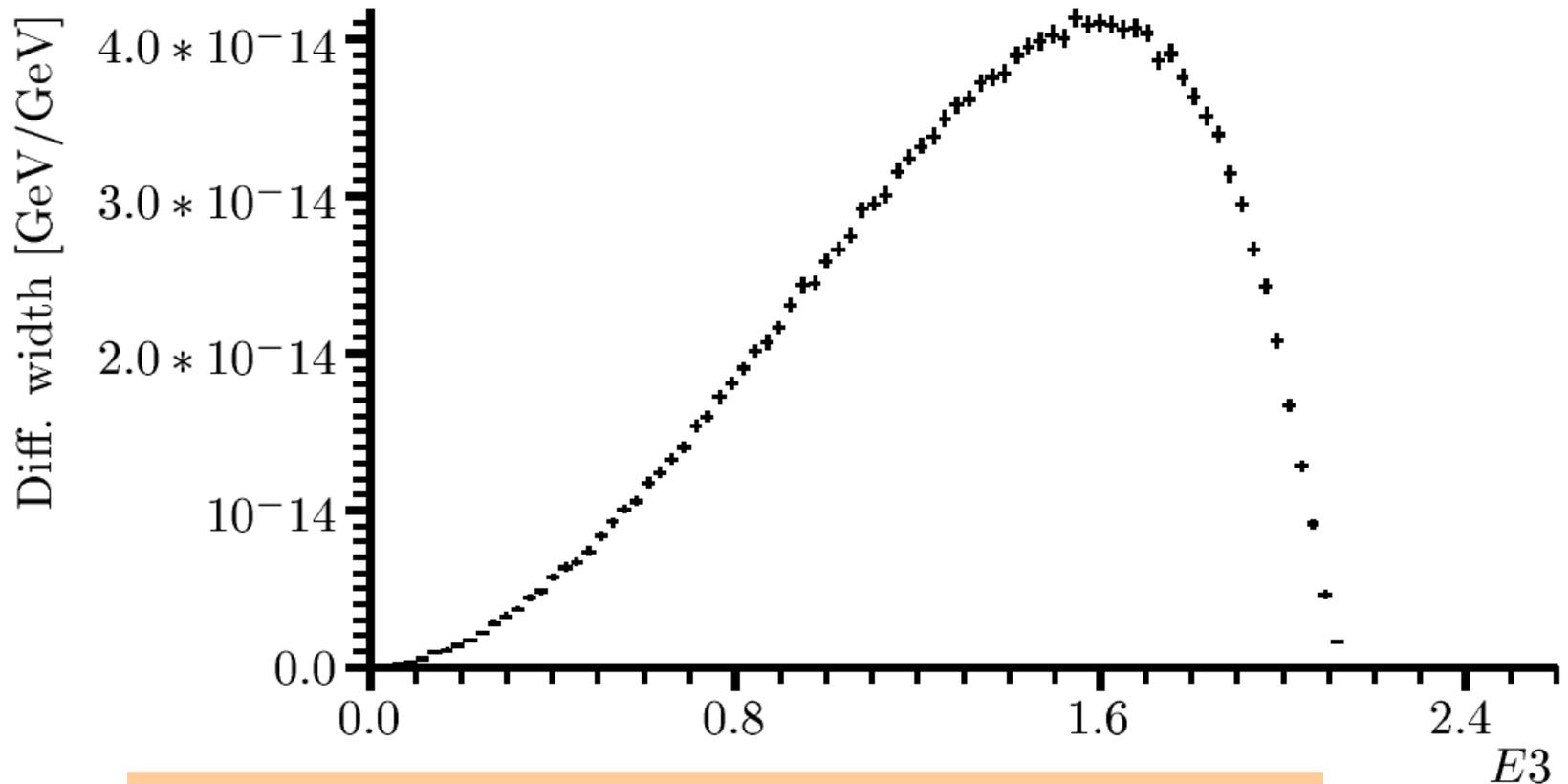
$$E_\gamma > 10 \text{ MeV}$$

$$\frac{\Gamma(\mu^- \rightarrow e^- \nu_\mu \bar{\nu}_e \gamma)}{\Gamma(\mu^- \rightarrow e^- \nu_\mu \bar{\nu}_e)} \approx 1.7\%$$

# $b$ -quark decay in CompHEP

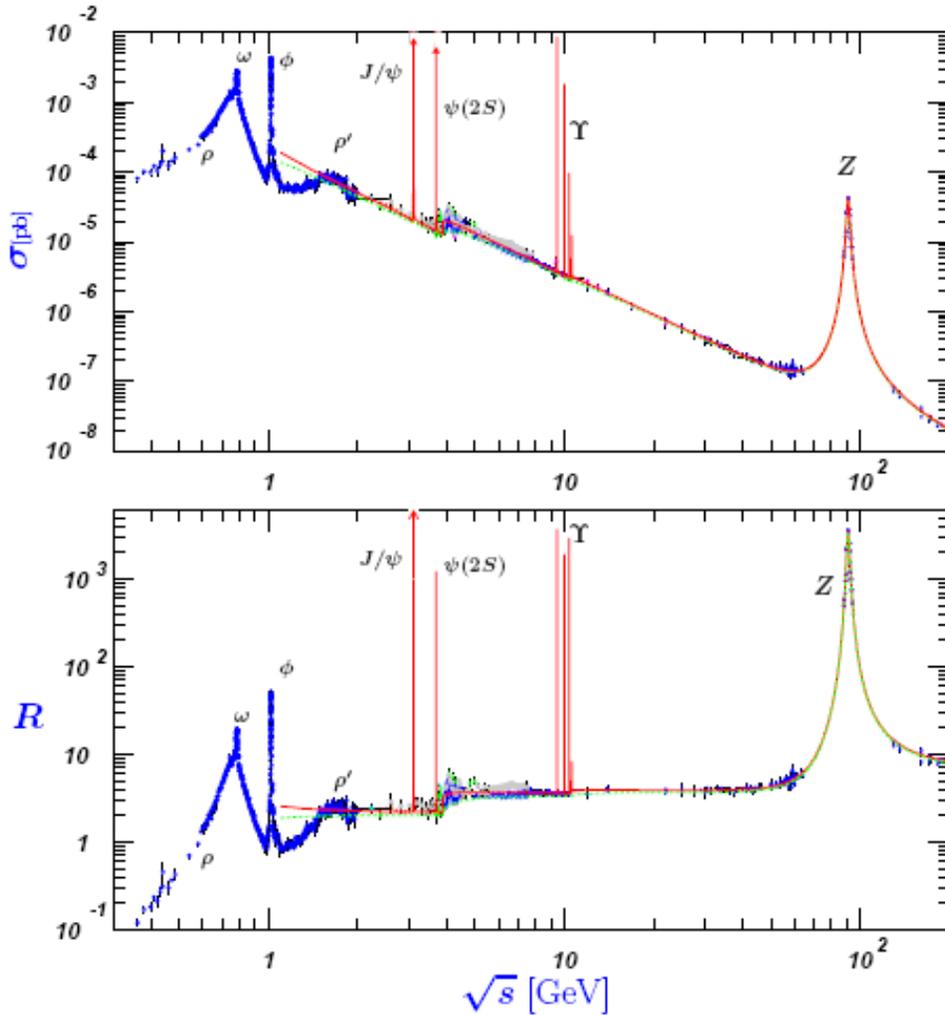
Electron energy spectrum in  $b \rightarrow c e \nu$

$b^- \rightarrow Ne, e, c$

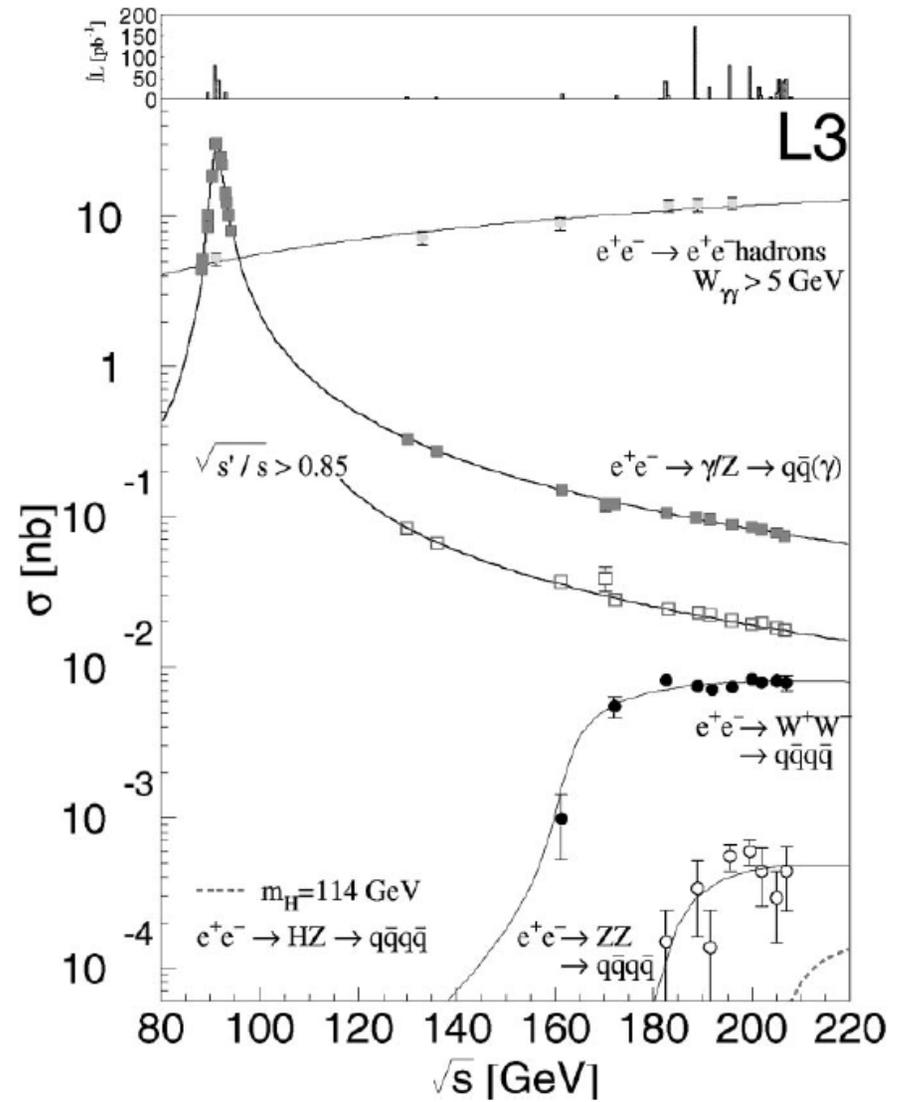


*Used to measure  $V_{cb}$ ,  $m_b$ , and  $m_c$ ...a long story!*

# $e^+e^-$ Scattering

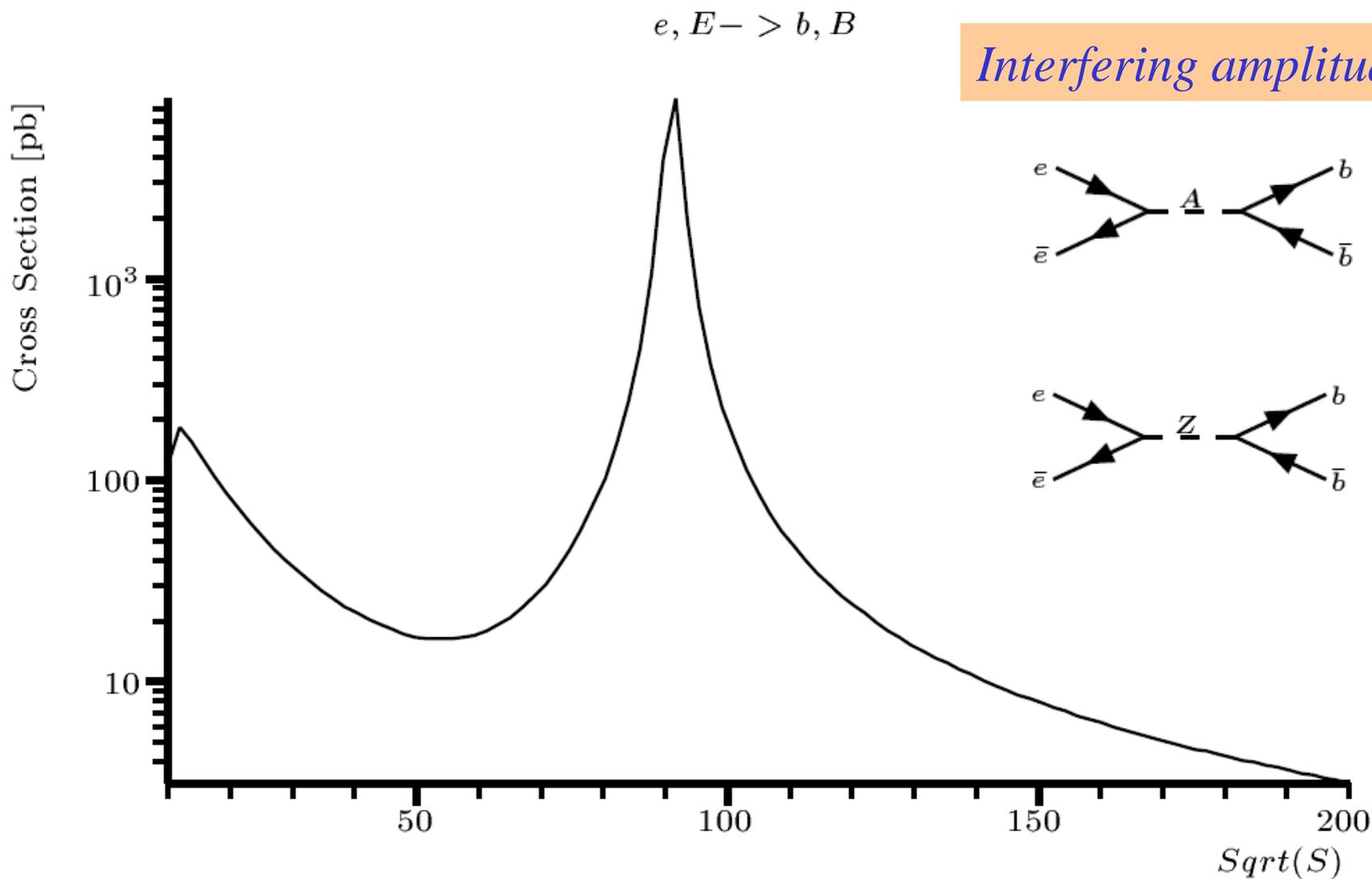


PDG 2005

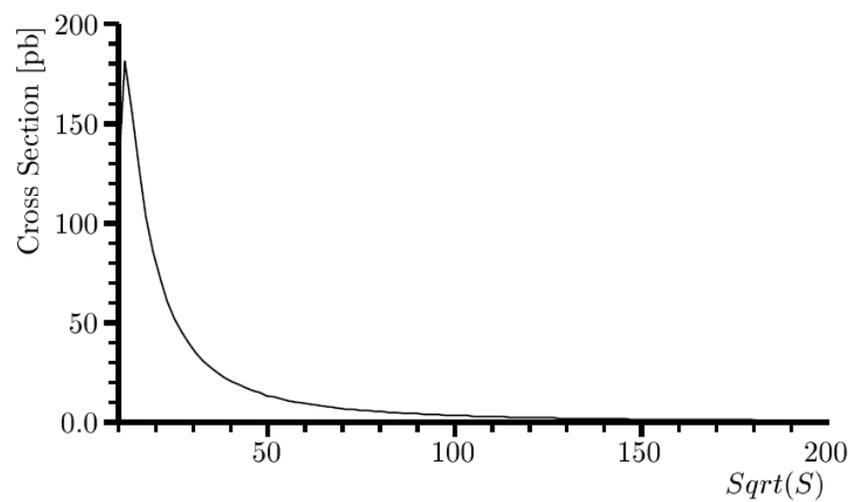


M.M. Kado and C.G. Tully, *Ann. Rev. Nucl. Part. Phys.*, Vol 52 (2002)

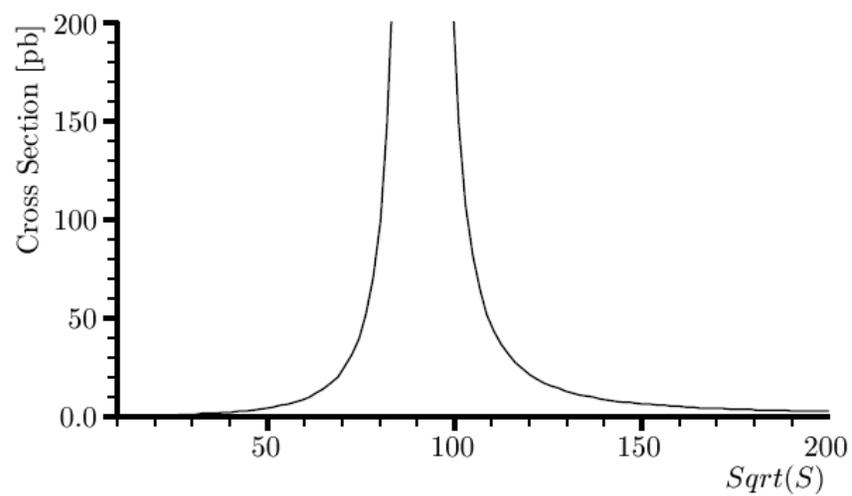
# Cross section vs. CM energy for $e^+e^- \rightarrow b\bar{b}$



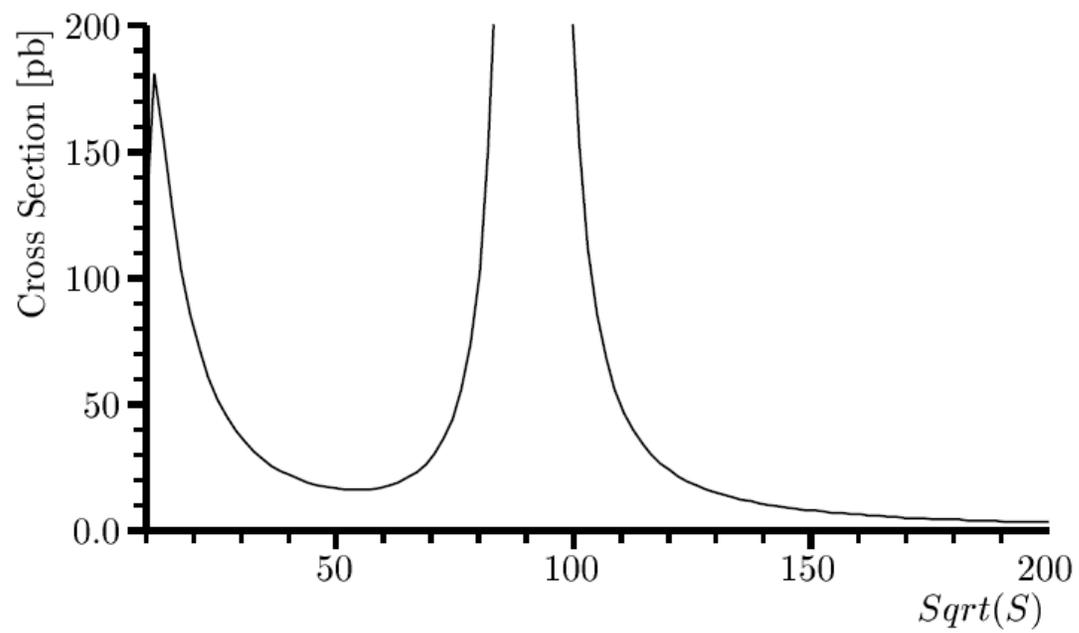
$e, E^- \rightarrow b, B$



$e, E^- \rightarrow b, B$

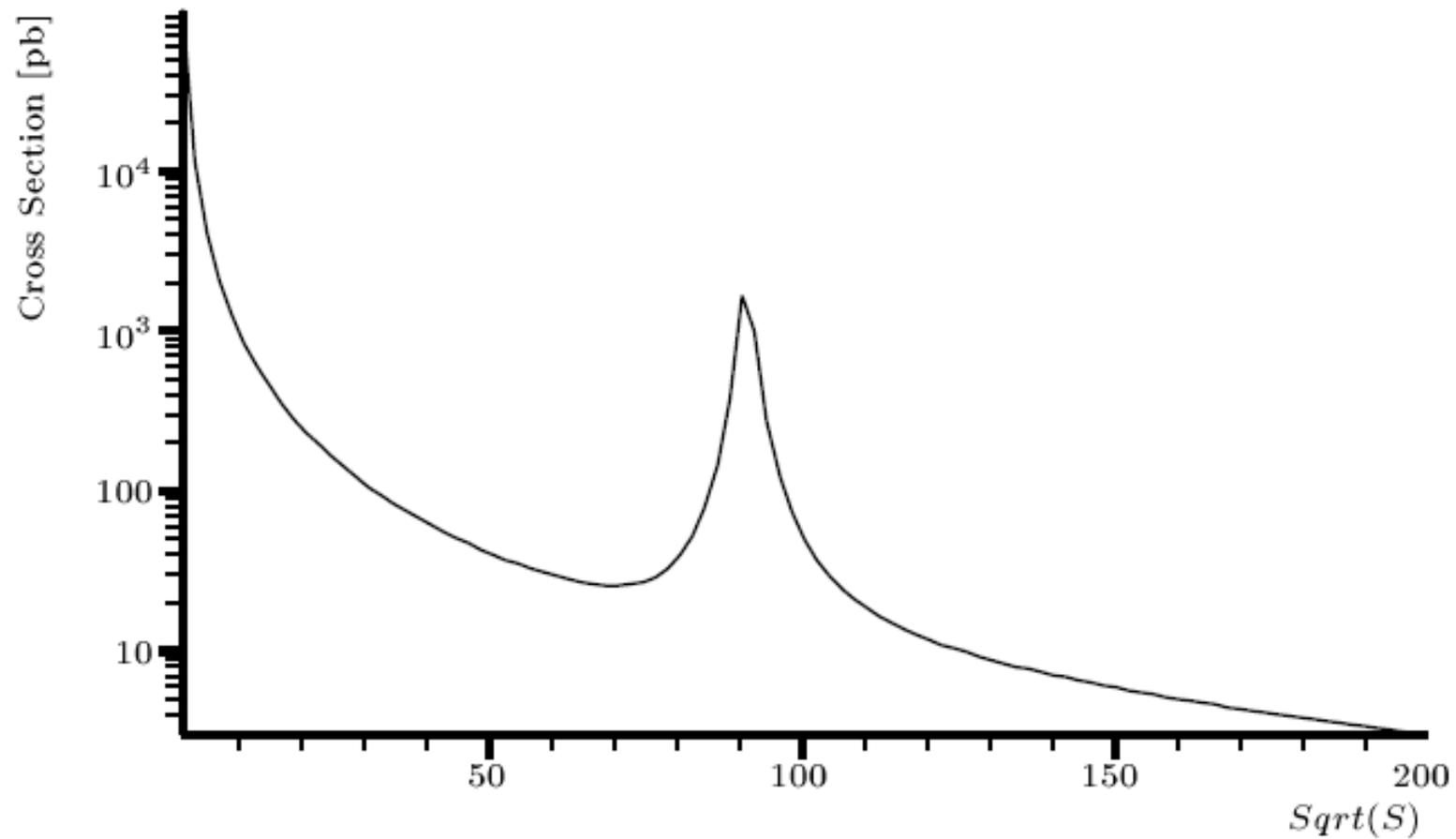


$e, E^- \rightarrow b, B$

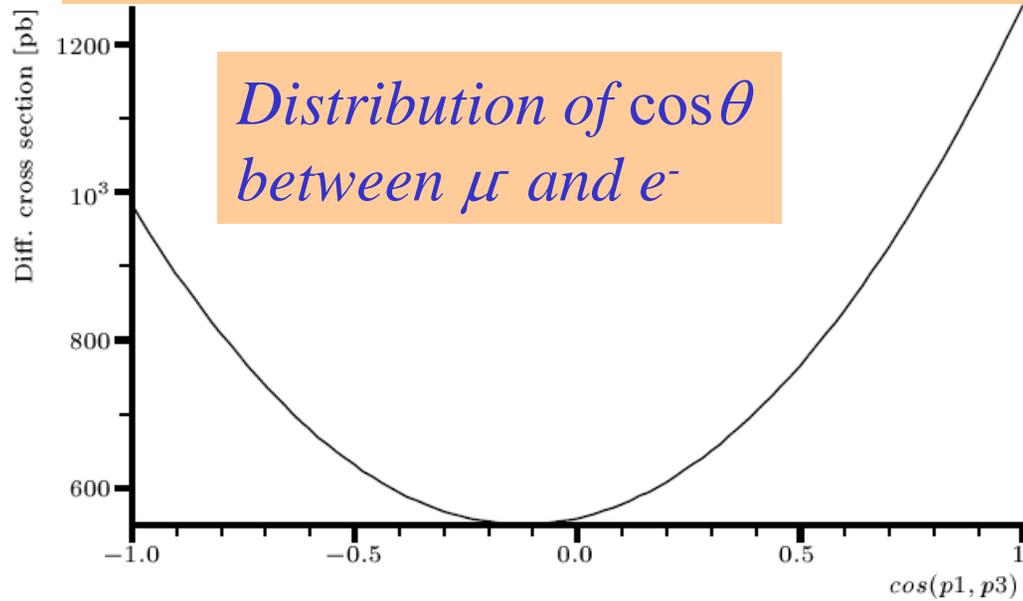


# Cross section vs. CM energy for $e^+e^- \rightarrow \mu^+\mu^-$

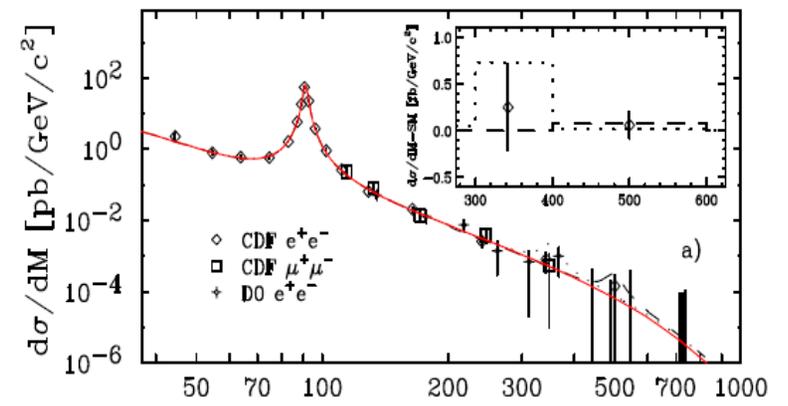
$$e, E- > m, M$$



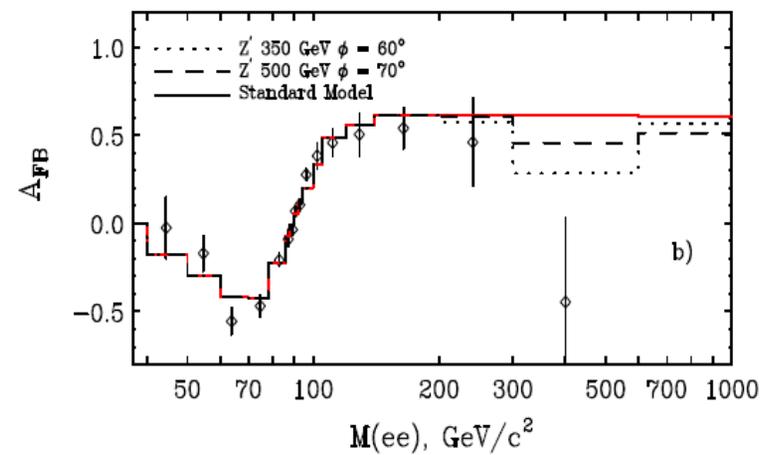
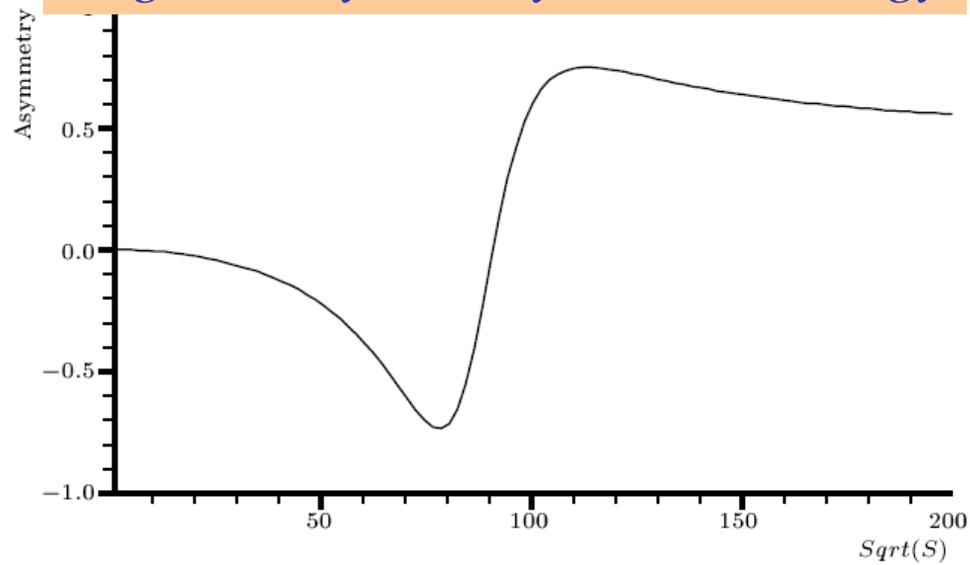
# $e^+e^- \rightarrow \mu^+ \mu^-$ angular distribution and forward-backward asymmetry



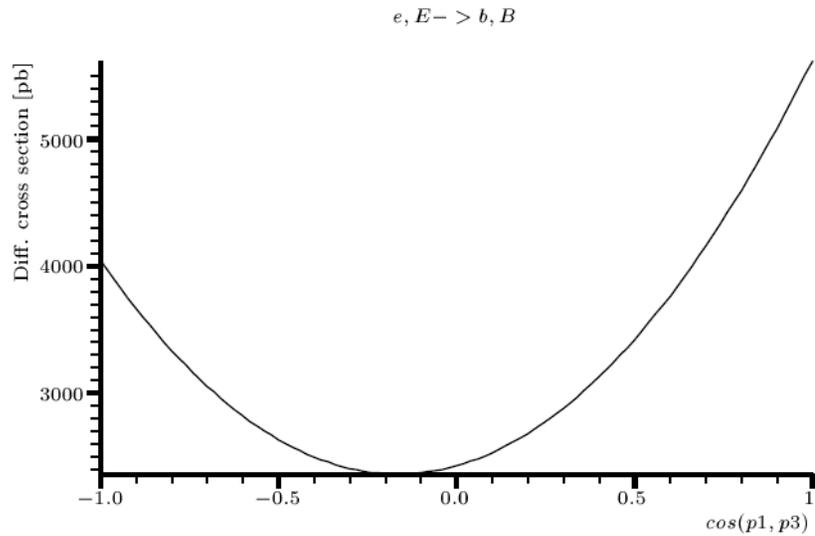
*Measurement was done at the Tevatron too! (hep-ex/0106047)*



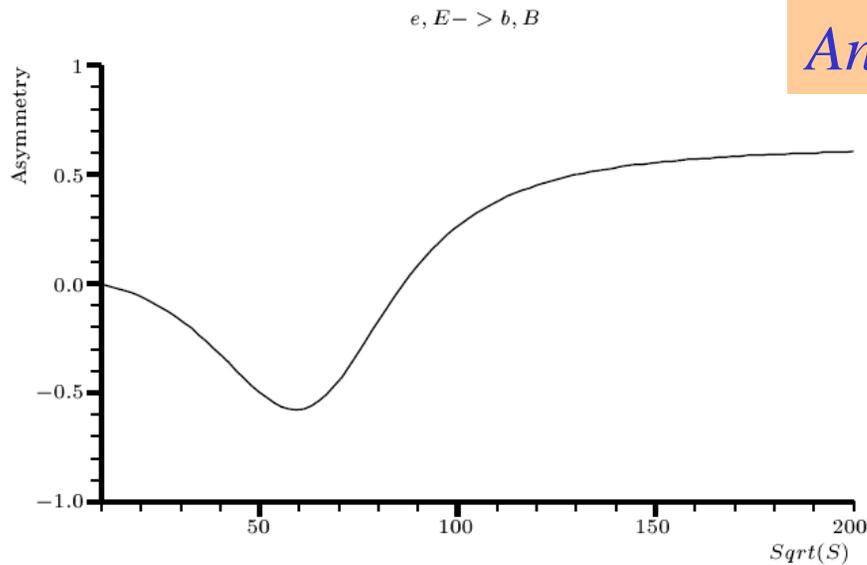
## Angular asymmetry vs. CM energy



# $e^+e^- \rightarrow b\bar{b}$ angular distribution and forward-backward asymmetry

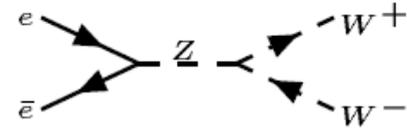
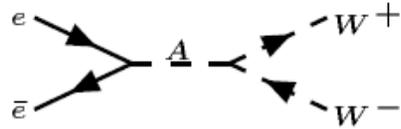
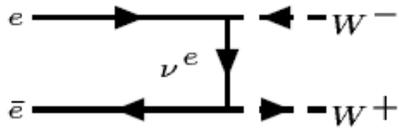


*Distribution of  $\cos\theta$   
between  $b$  and  $e^-$*

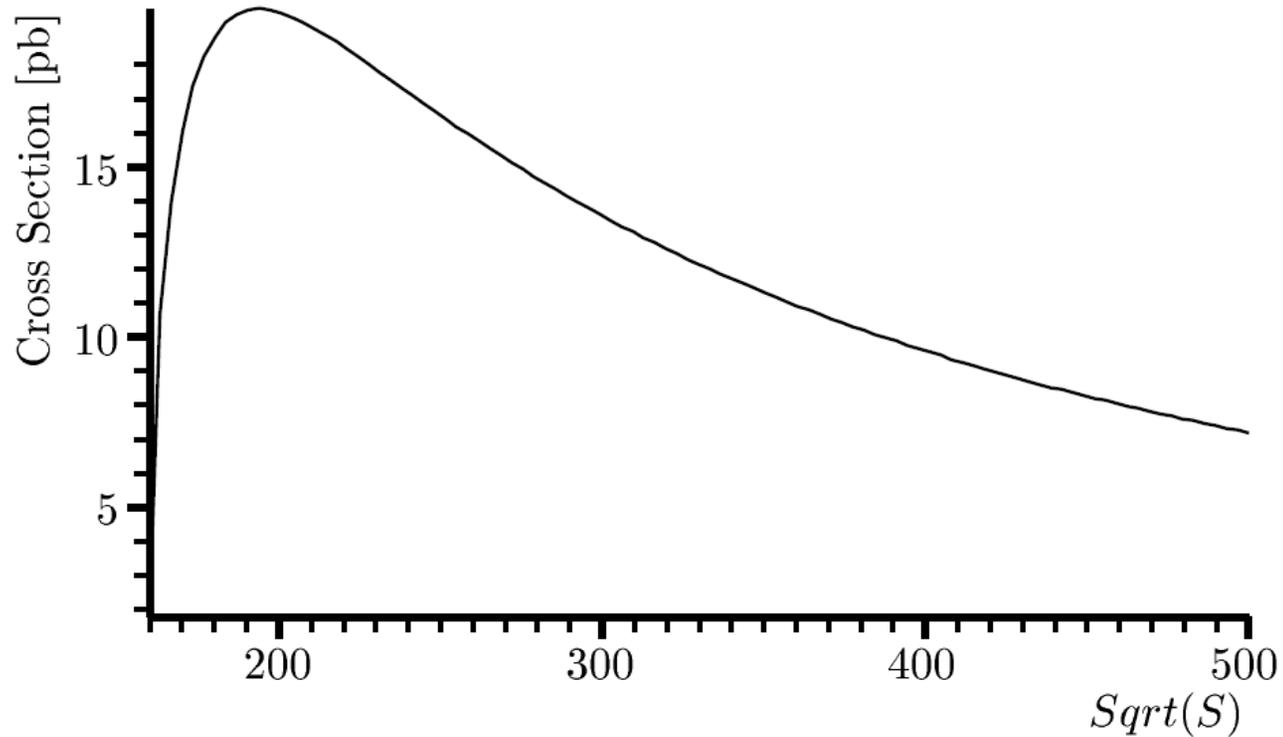


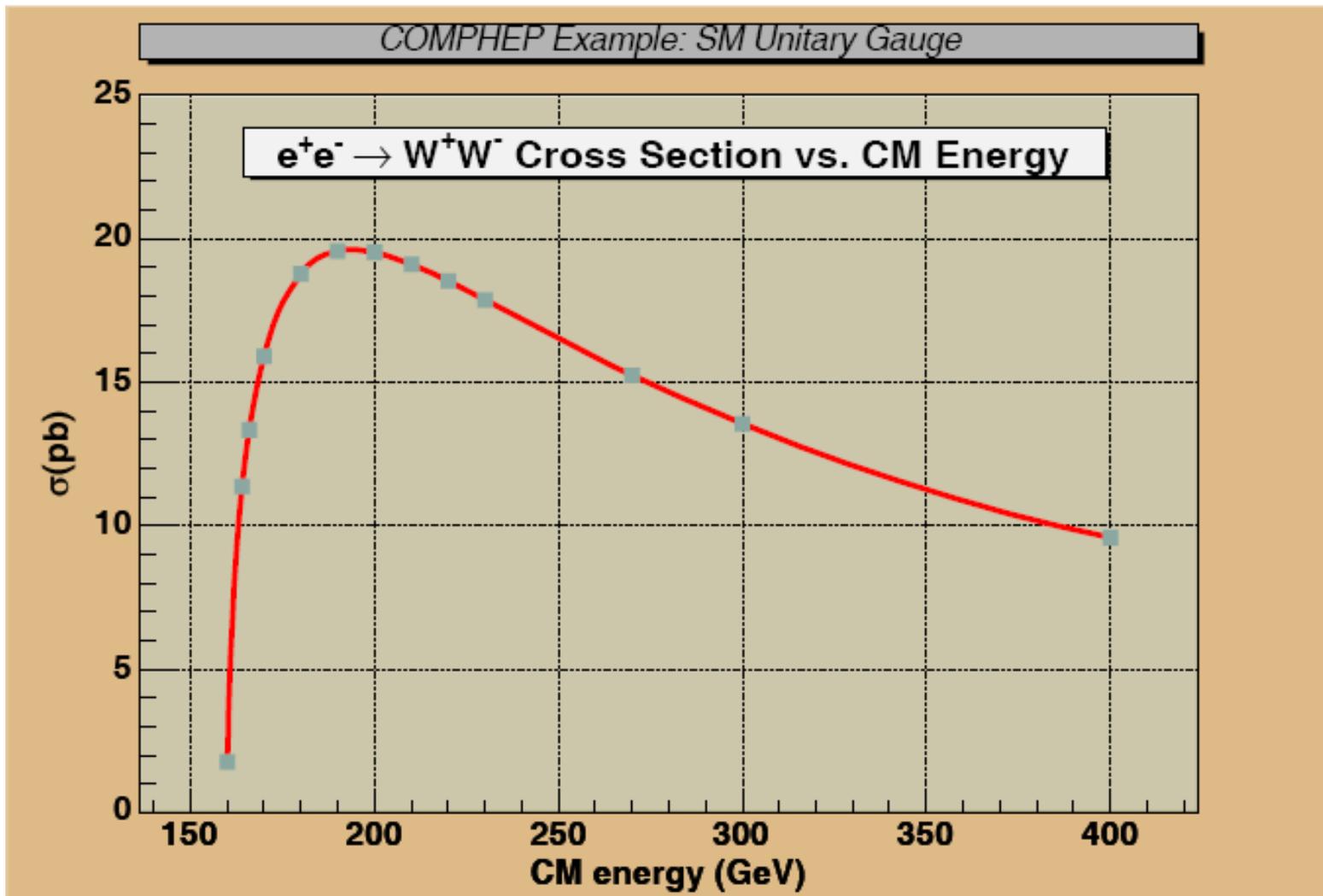
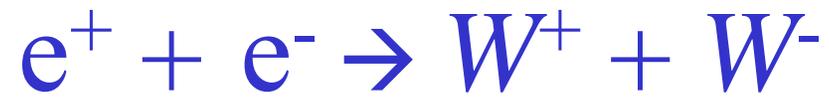
*Angular asymmetry vs. CM energy*

# Cross section vs. CM energy for $e^+e^- \rightarrow W^+W^-$



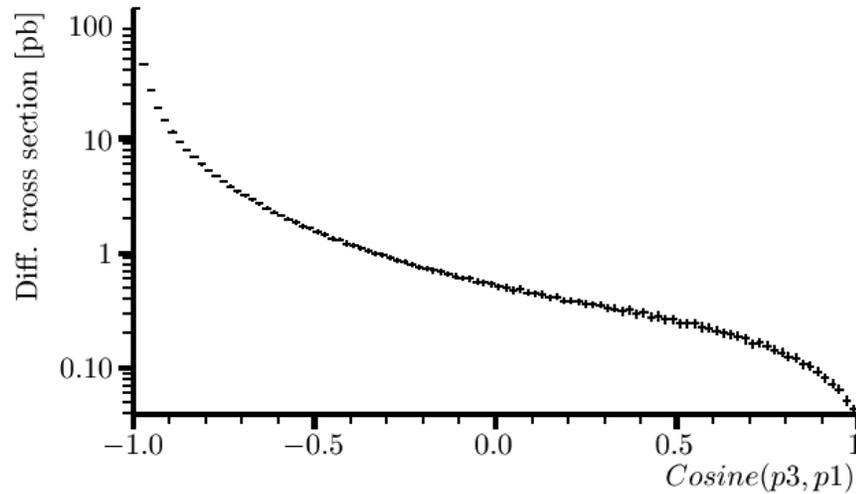
$$e, E^- \rightarrow W^+, W^-$$



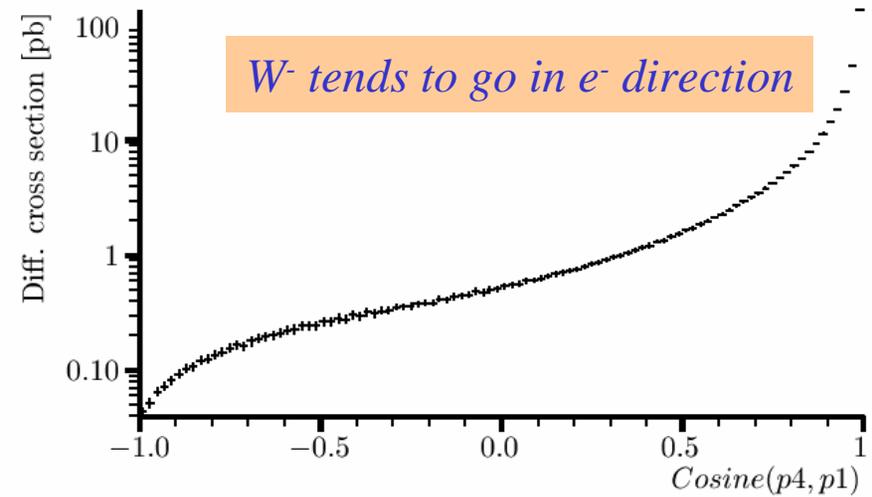


# Angular Distributions and Asymmetry for $e^+e^- \rightarrow W^+W^-$

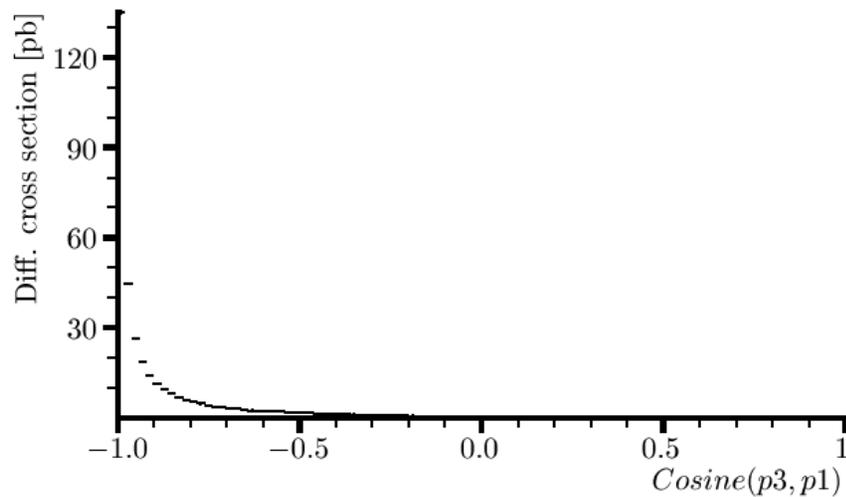
$e, E^- \rightarrow W^+, W^-$



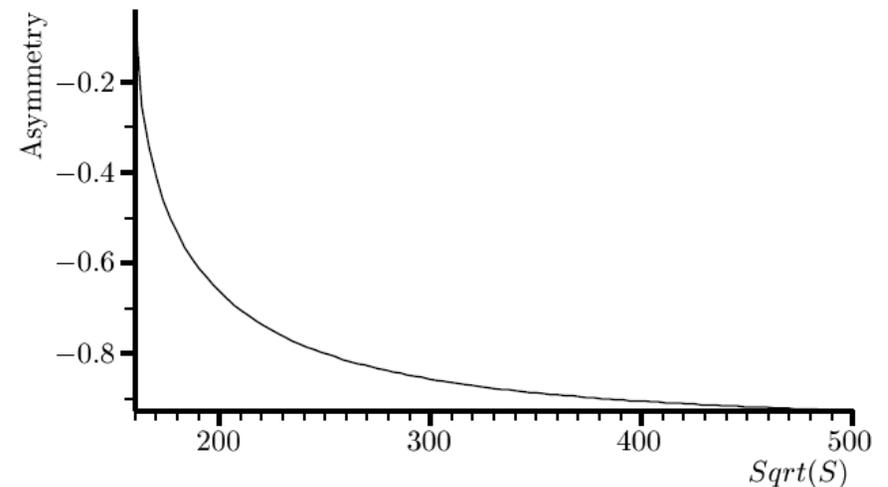
$e, E^- \rightarrow W^+, W^-$



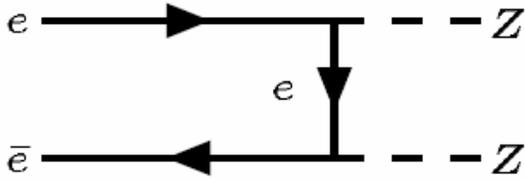
$e, E^- \rightarrow W^+, W^-$



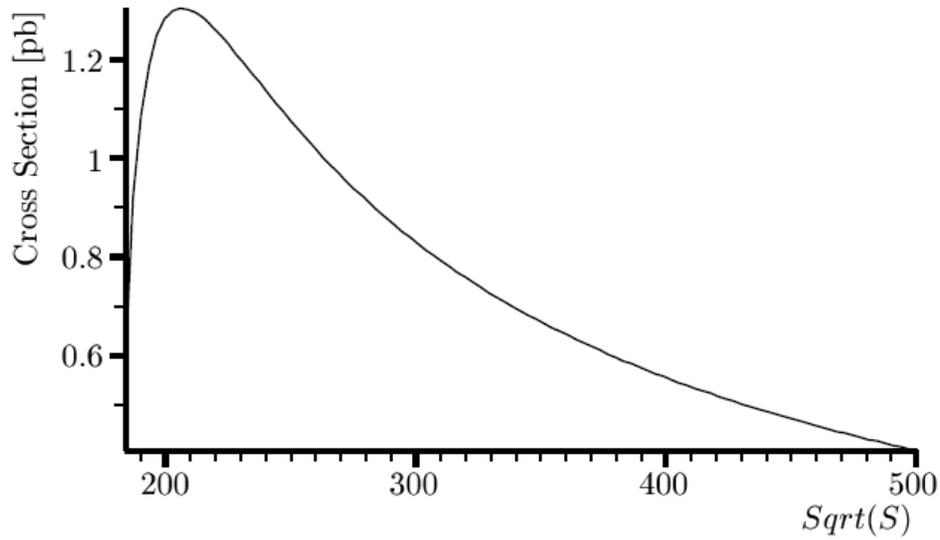
$e, E^- \rightarrow W^+, W^-$



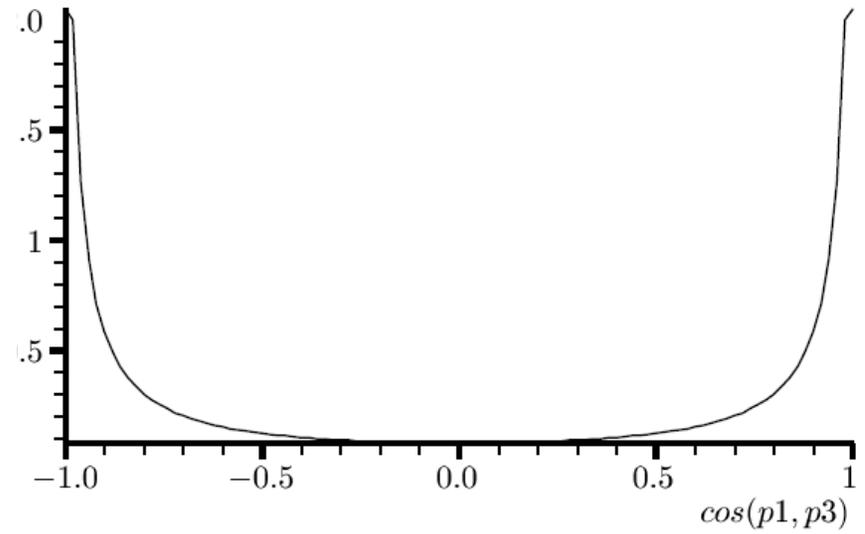
$$e^+ + e^- \rightarrow Z + Z$$



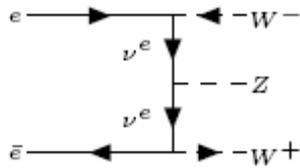
$e, E- \rightarrow Z, Z$



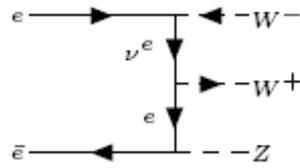
$e, E- \rightarrow Z, Z$



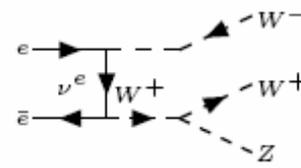
# CompHEP Diagrams for $e^+e^- \rightarrow W^+W^-Z$



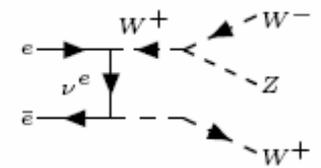
diagr.1



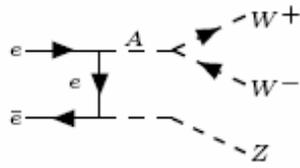
diagr.2



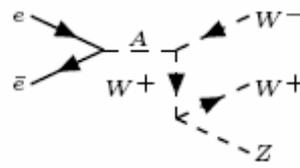
diagr.3



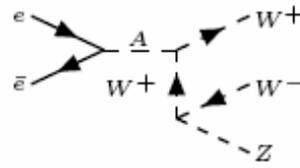
diagr.4



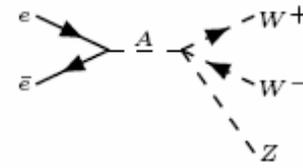
diagr.5



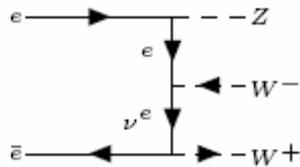
diagr.6



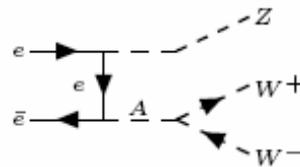
diagr.7



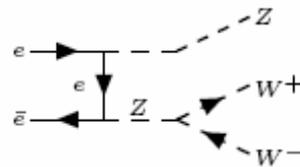
diagr.8



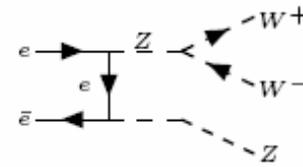
diagr.9



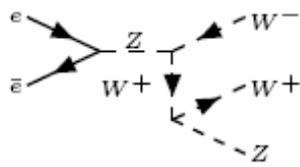
diagr.10



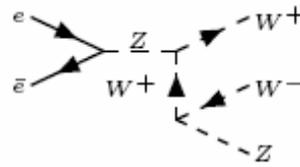
diagr.11



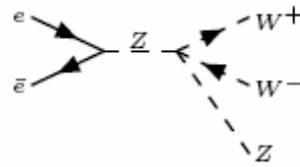
diagr.12



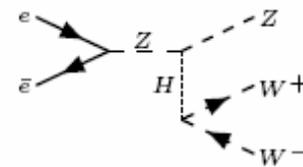
diagr.13



diagr.14



diagr.15

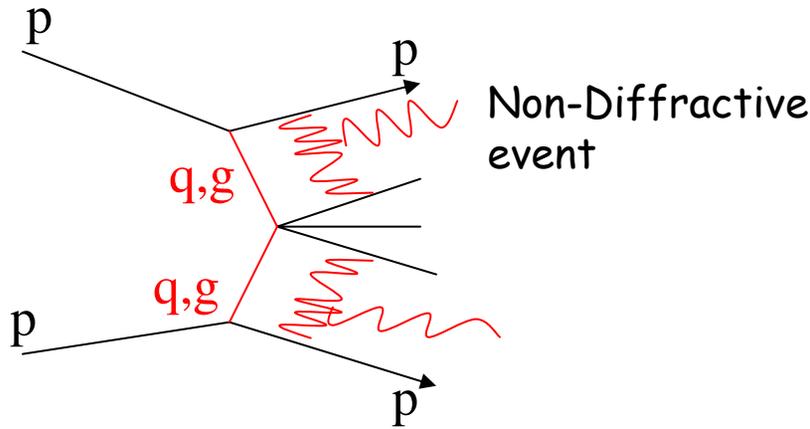
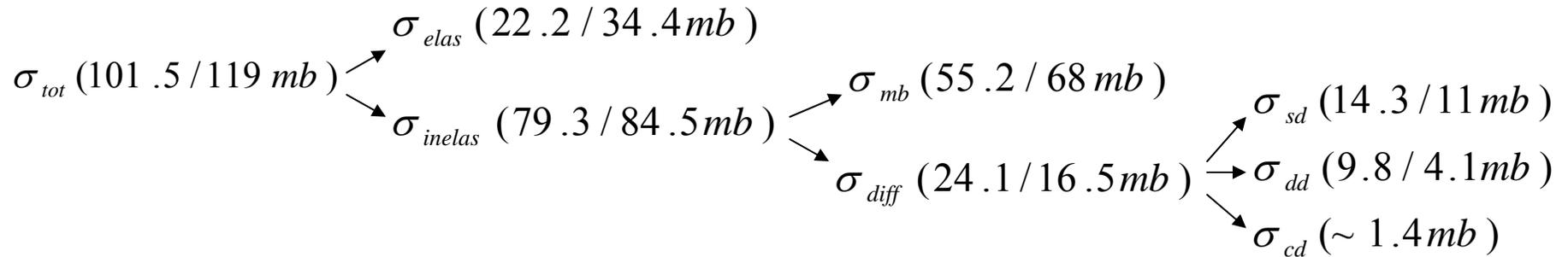


diagr.16

# pp Scattering Cross Sections

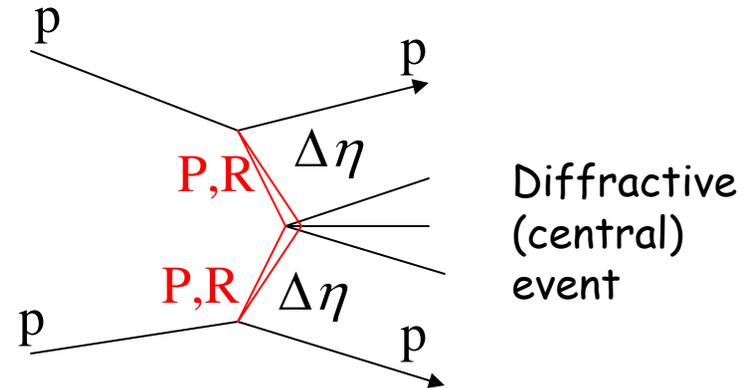
from talk by A. Sobol at US CMS meeting, April 7, 2006:

PYTHIA6.205/PHOJET1.12 predictions for cross sections at  $\sqrt{s}=14$  TeV



Exchange of color triplets, octets

- exponential suppression of rapidity gaps (gaps filled by color exchange in hadronization)



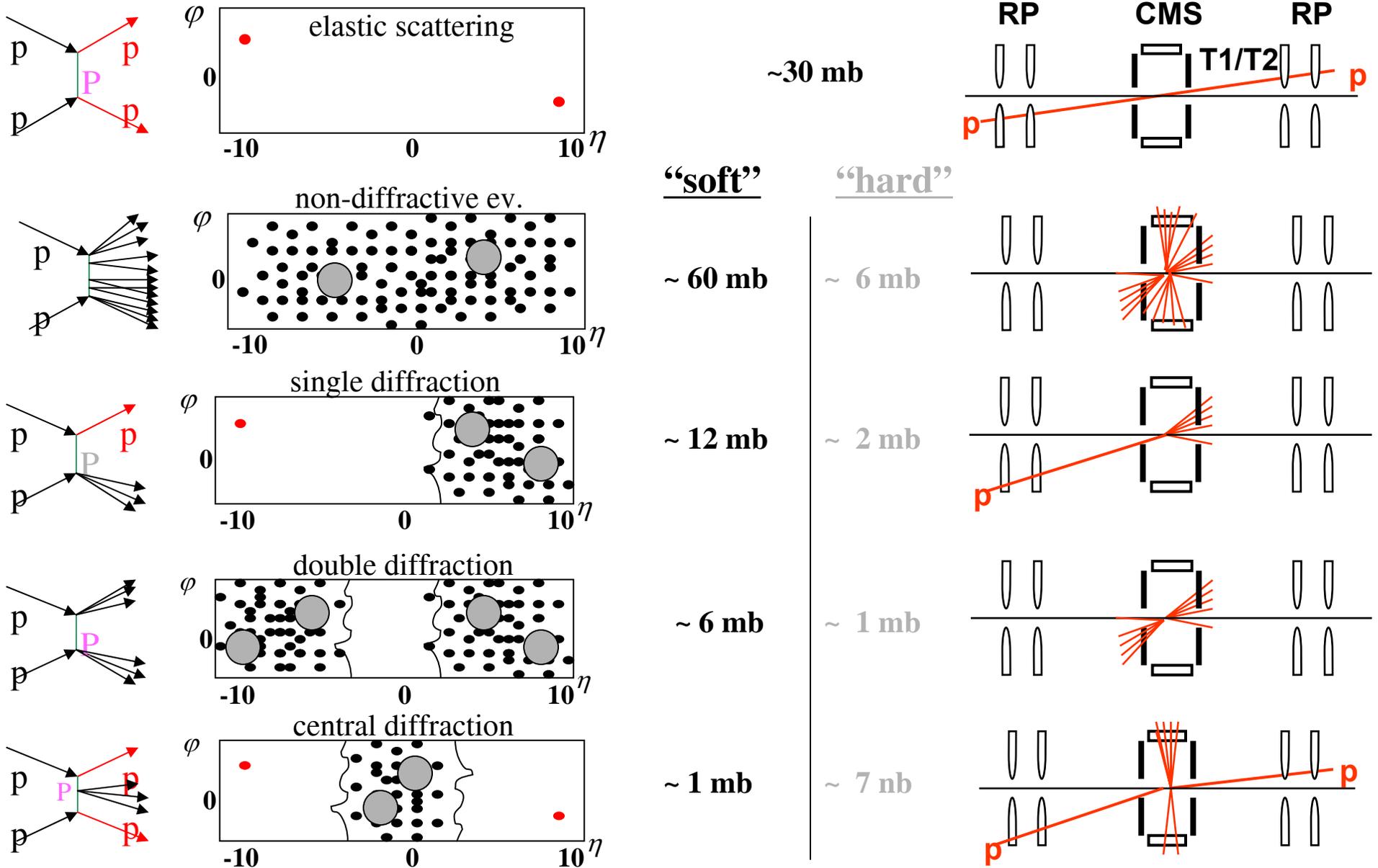
Exchange of color singlets:  
Reggeons, Pomerons

- rapidity gaps  $\Delta\eta > 3-4$
- momentum loss of the leading protons

$$\xi = \frac{\Delta p}{p} < 0.05 - 0.1$$

# Diffraction: events topologies

from talk by A. Sobol, US CMS meeting, April 7, 2006



# CompHEP: $p + p$ Scattering

```
CompHEP version 4.4.3
Model: SM, unitary gauge

List of structure functions

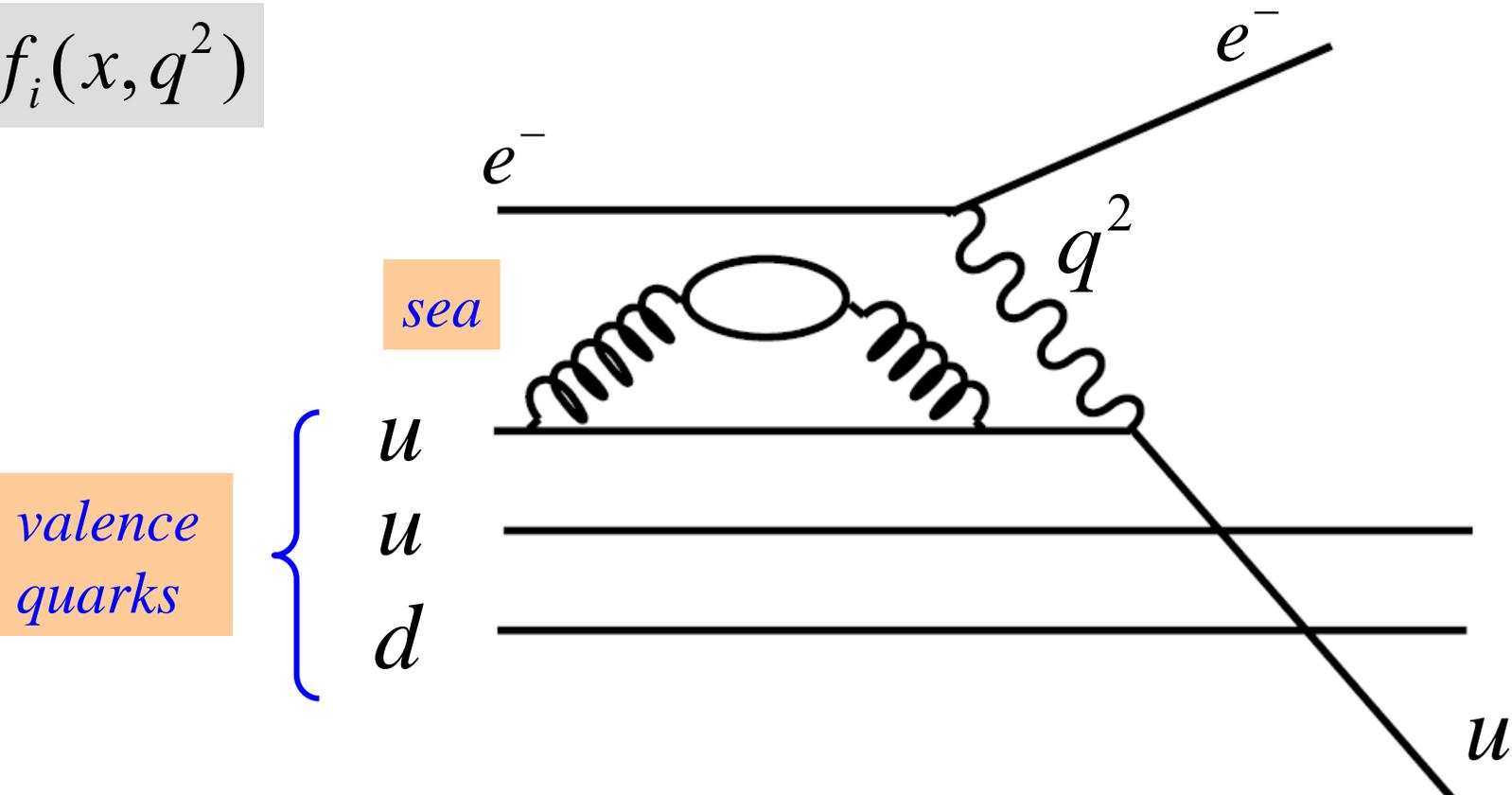
0: OFF
1: WWA (m=0.000511 Ch=-1 Q=100)
2: Laser Photons
3: ISR(100 Beamstr.:OFF)
10: cteq6m(proton)
11: cteq6m(anti-proton)
12: cteq6l1(proton)
13: cteq6l1(anti-proton)
14: cteq6d(proton)
15: cteq6d(anti-proton)
16: cteq5m1(proton)
17: cteq5m1(anti-proton)

PgDn

Enter 1st Beam: p
Enter 1st Beam Energy (GeV) : 7000.000000
Enter 2nd Beam: p
Enter 2nd Beam Energy (GeV) : 7000.000000
Enter PDF number : 12
```

# Proton Structure Functions

$$f_i(x, q^2)$$



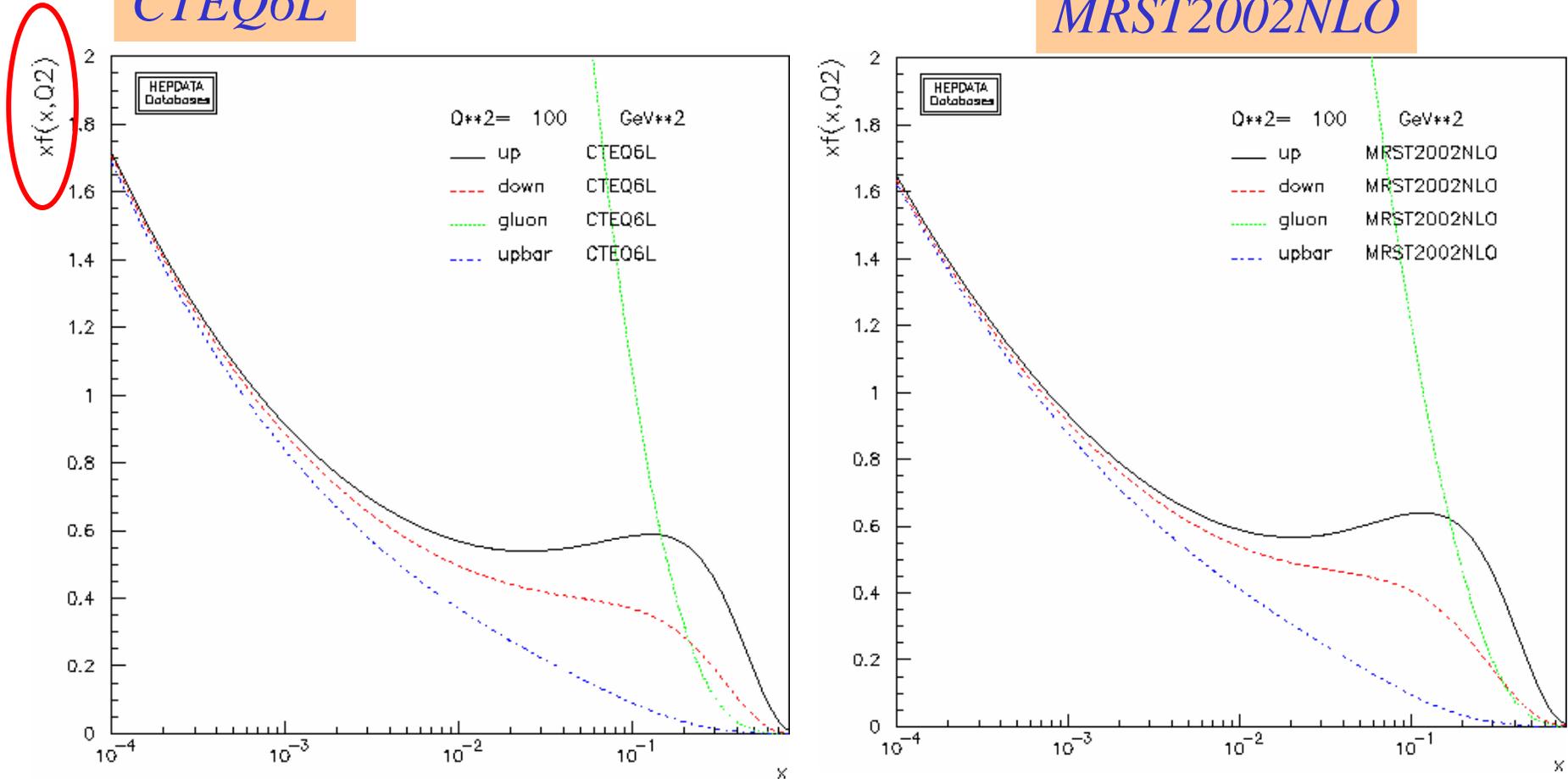
Prob to find a parton of type  $i$  carrying a fraction of the proton's longitudinal momentum  $x = p_L^i / p_L$

Cannot be calculated from 1st principles: extracted from data.

# Structure functions from Durham HEP Database

*CTEQ6L*

*MRST2002NLO*

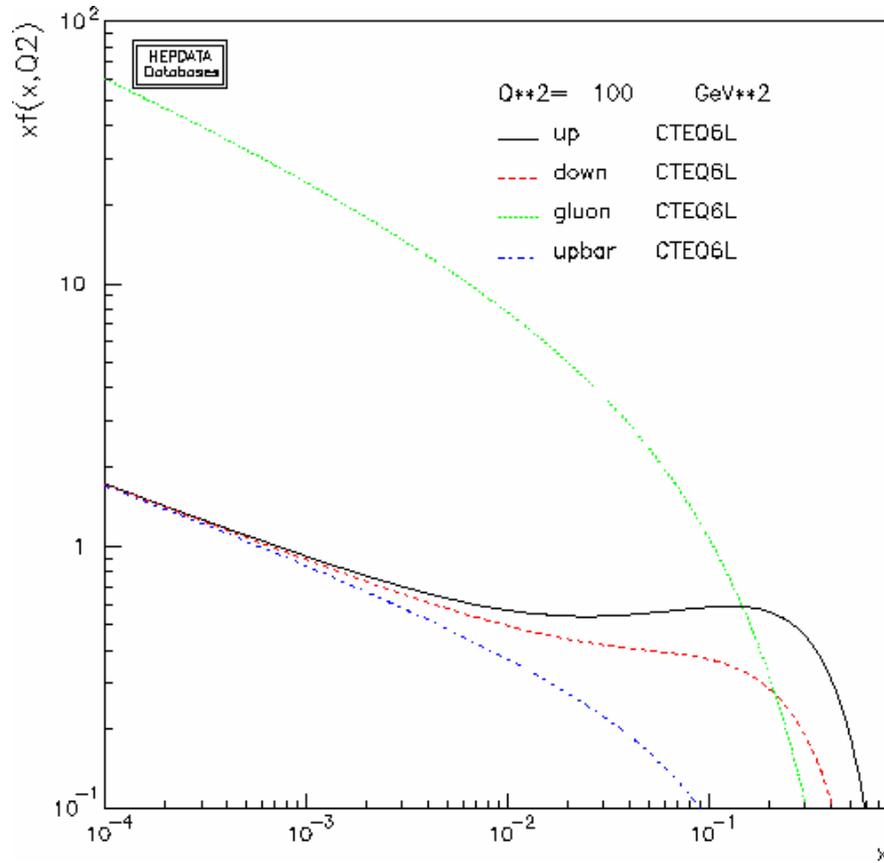


<http://durpdg.dur.ac.uk/HEPDATA>

# Structure functions (Durham HEP database)

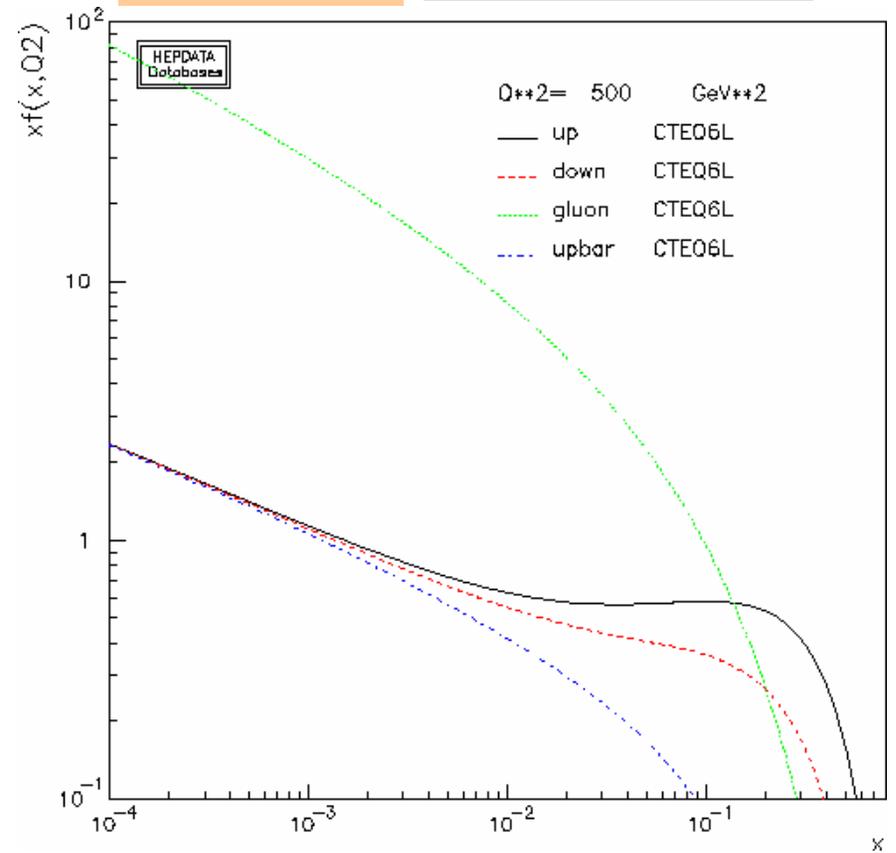
*CTEQ6L*

$Q^2 = 100 \text{ GeV}^2$



*CTEQ6L*

$Q^2 = 500 \text{ GeV}^2$



<http://durpdg.dur.ac.uk/HEPDATA>

# $p + p \rightarrow G + G$ at 14 TeV

CompHEP version 4.4.3

**Model:** SM, unitary gauge

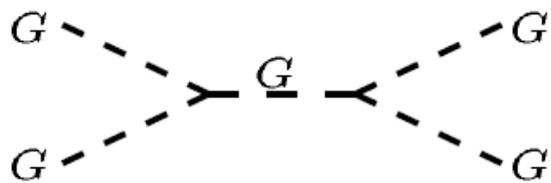
**Process:** p,p -> G,G

**Feynman diagrams**

18 diagrams in 9 subprocesses are constructed.  
0 diagrams are deleted.

NN	Subprocess	Del	Rest
*			
1	u,U -> G,G	0	2
2	d,D -> G,G	0	2
3	U,u -> G,G	0	2
4	D,d -> G,G	0	2
5	s,S -> G,G	0	2
6	c,C -> G,G	0	2
7	S,s -> G,G	0	2
8	C,c -> G,G	0	2
9	G,G -> G,G	0	2

F1-Help F2-Man F3-Model F5-Switches F6-Results F7-Del F8-UnDel F9-Quit



Apply cut before computing cross section:  $p_t(G) > 35 \text{ GeV}$

# $p + p \rightarrow G + G$ at 14 TeV

```
CompHEP version 4.4.3

Process: p,p -> G,G (9 subprocesses)
(sub)Process: G,G -> G,G
Monte Carlo session: 1(begin)

#IT   Cross section [pb]   Error %   nCall   chi**2
1     6.6512E+07           6.85E+01  9792
2     2.8964E+07           3.71E+01  9792
3     5.2245E+07           1.54E+01  9792
4     4.8176E+07           2.46E+00  9792
5     5.0217E+07           1.44E+00  9792
< >  4.9615E+07           1.24E+00  48960  2
6     4.9609E+07           1.29E+00  9792
7     4.9563E+07           1.04E+00  9792
8     5.1268E+07           2.14E+00  9792
9     5.0072E+07           1.22E+00  9792
10    5.0284E+07           1.20E+00  9792
< >  4.9894E+07           5.16E-01  97920  1
```

Vegas

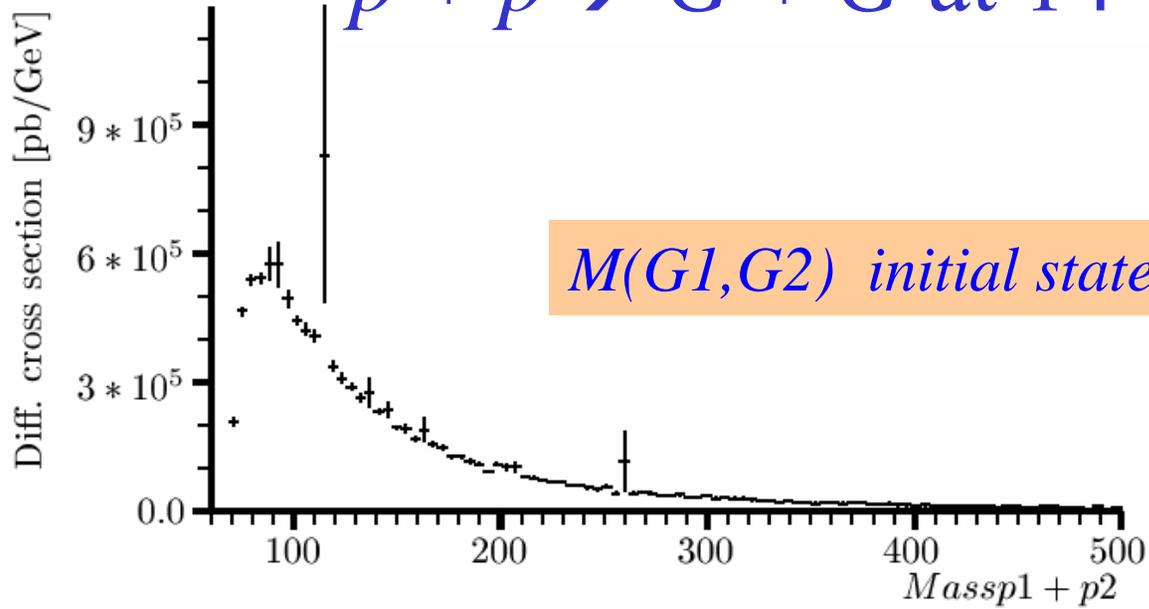
Start integration

Integration is over  
Press any key

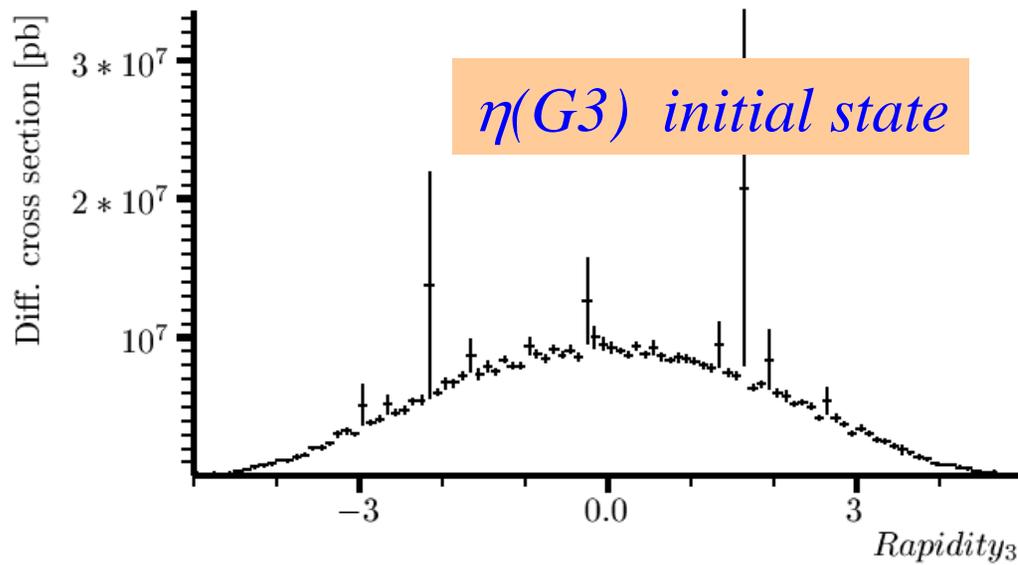
$$\sigma(pp[GG] \rightarrow GG) \approx 5 \times 10^7 \text{ pb} \approx 0.05 \text{ mb}$$

LHC

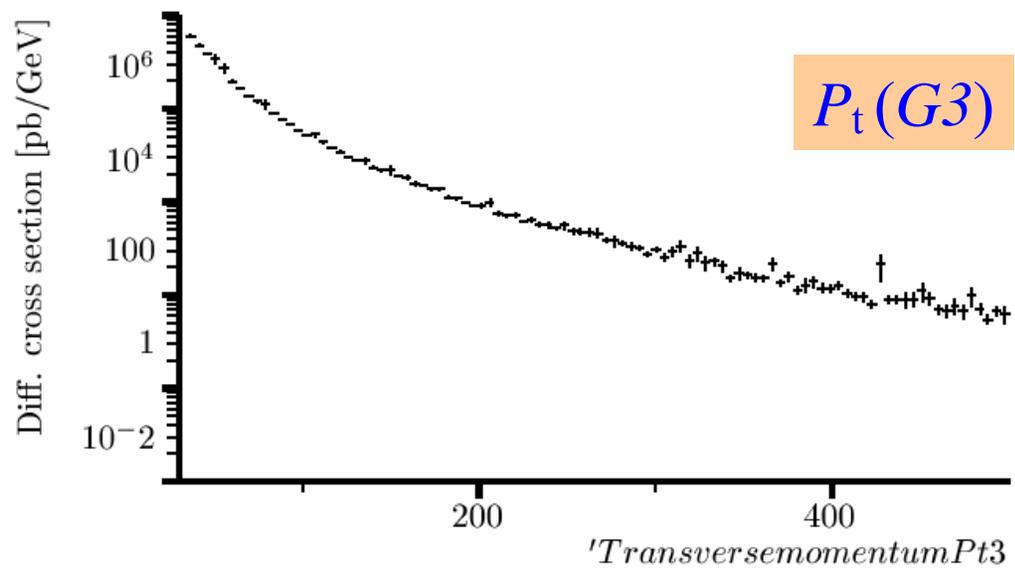
# $p + p \rightarrow G + G$ at 14 TeV



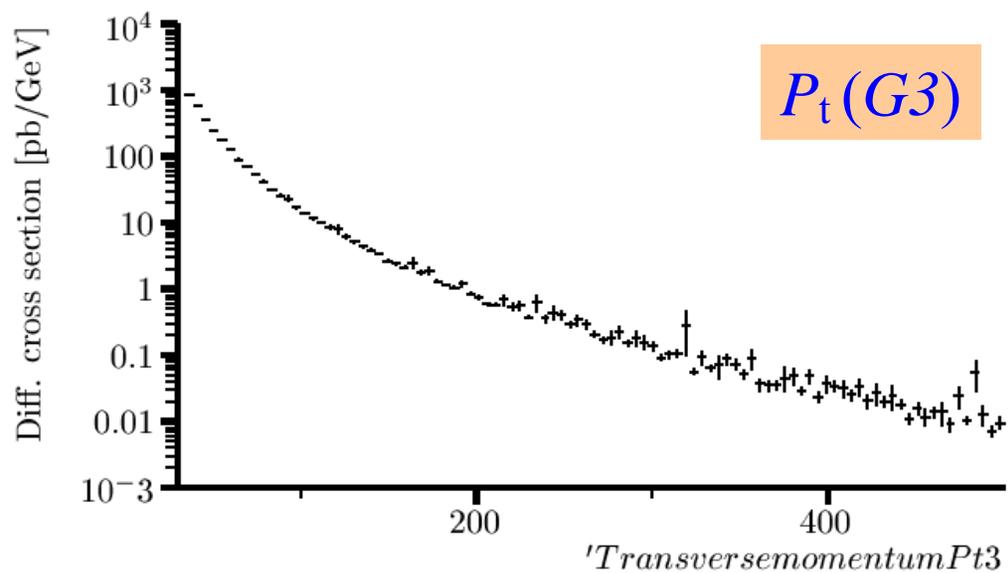
$G, G \rightarrow G, G$



$G, G- \rightarrow G, G$

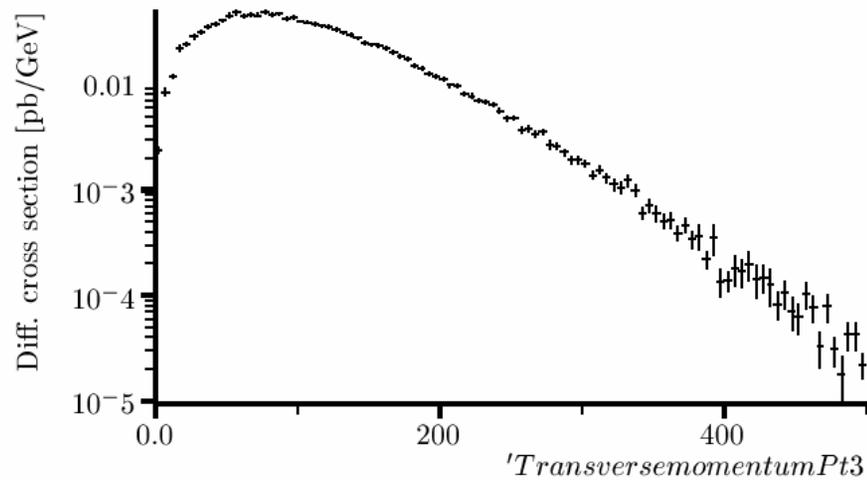
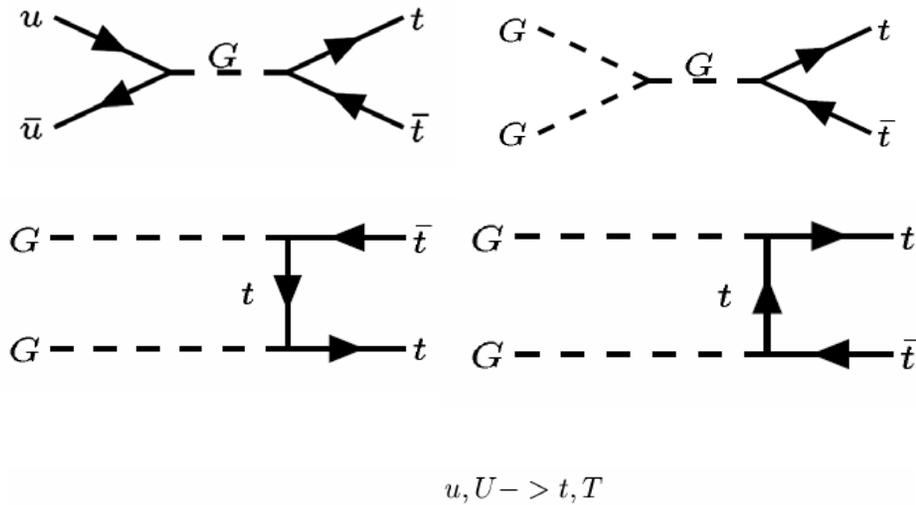


$u, U- \rightarrow G, G$



$$p + \bar{p} \rightarrow t + \bar{t}$$

CompHEP at  $\sqrt{s} = 2.0$  TeV



Process	$\sigma(\text{pb})$
$u\bar{u} \rightarrow t\bar{t}$	6.88
$d\bar{d} \rightarrow t\bar{t}$	1.28
$gg \rightarrow t\bar{t}$	0.53
$\bar{u}u \rightarrow t\bar{t}$	0.014
Total	8.7

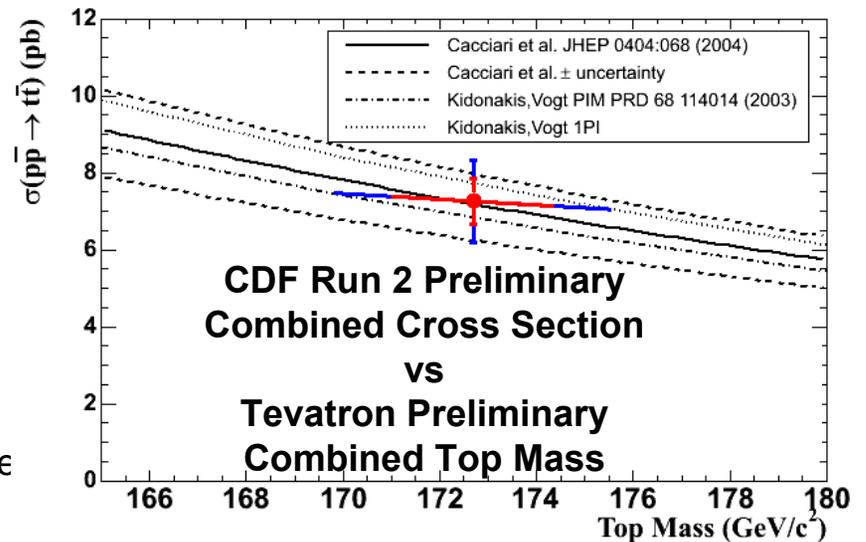
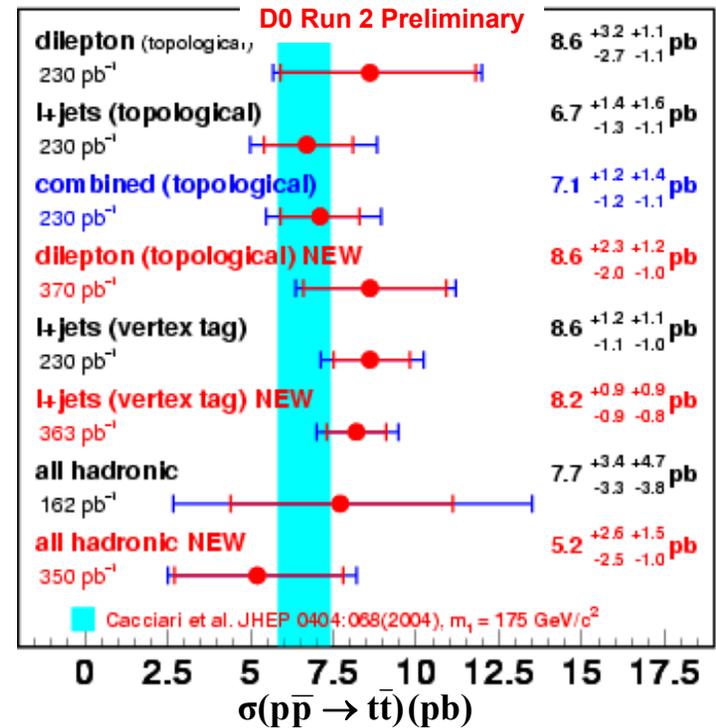
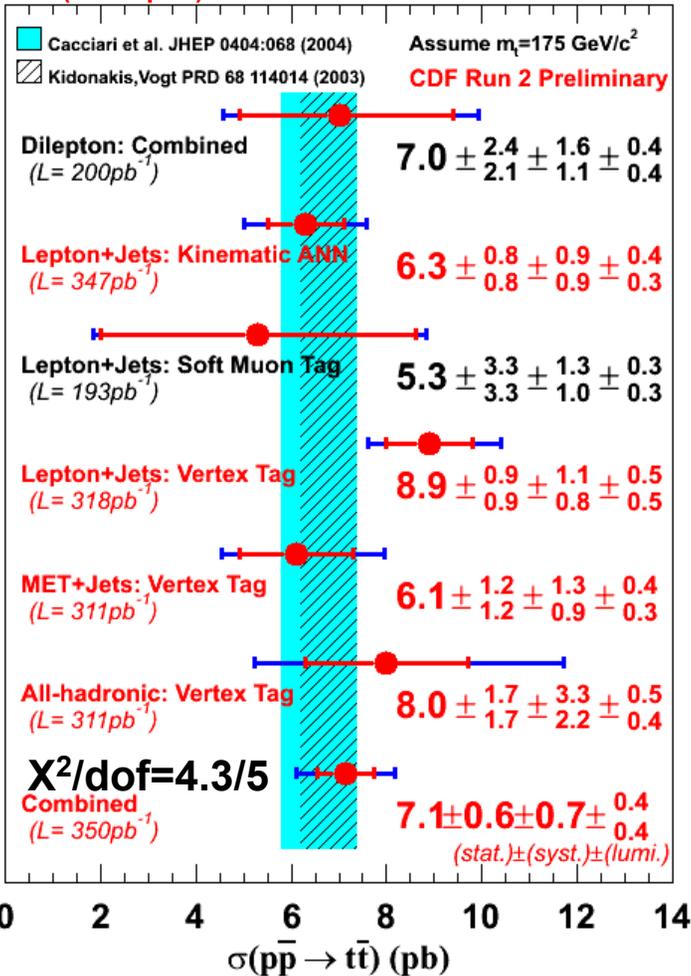
$$m_t = 174.3 \text{ GeV}$$

# Top Pair Production Rate

*Evelyn Thomson talk at PANIC 2005*

- Are measurements in different final states consistent with each other and with theory?

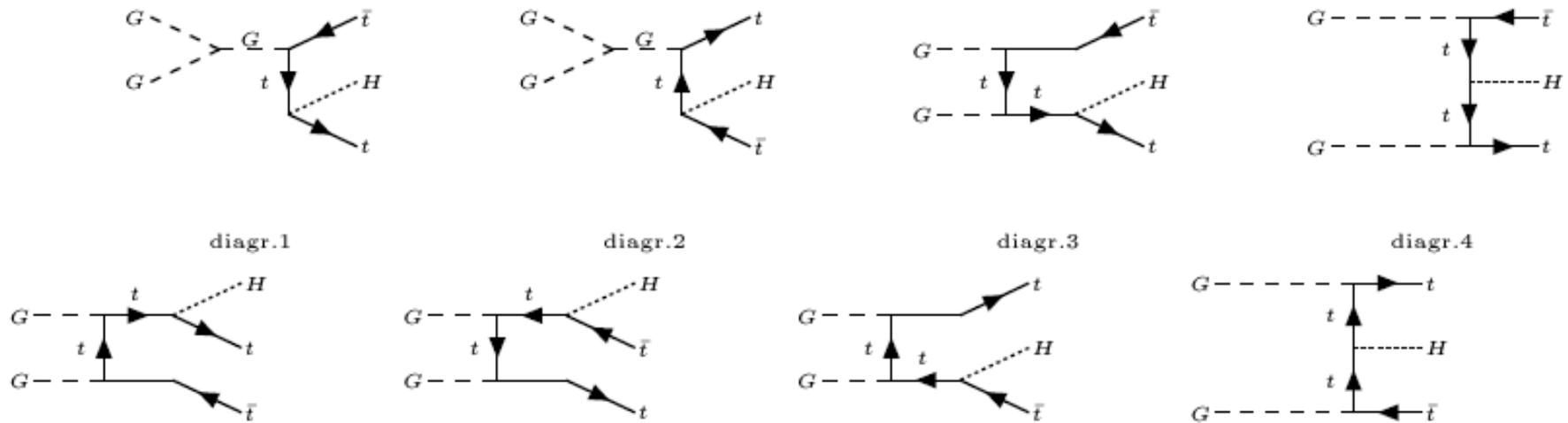
**Dilepton NEW**  
( $L=360\text{pb}^{-1}$ )  **$10.1 \pm 2.2 \pm 1.3 \pm 0.6$**



PAP Me

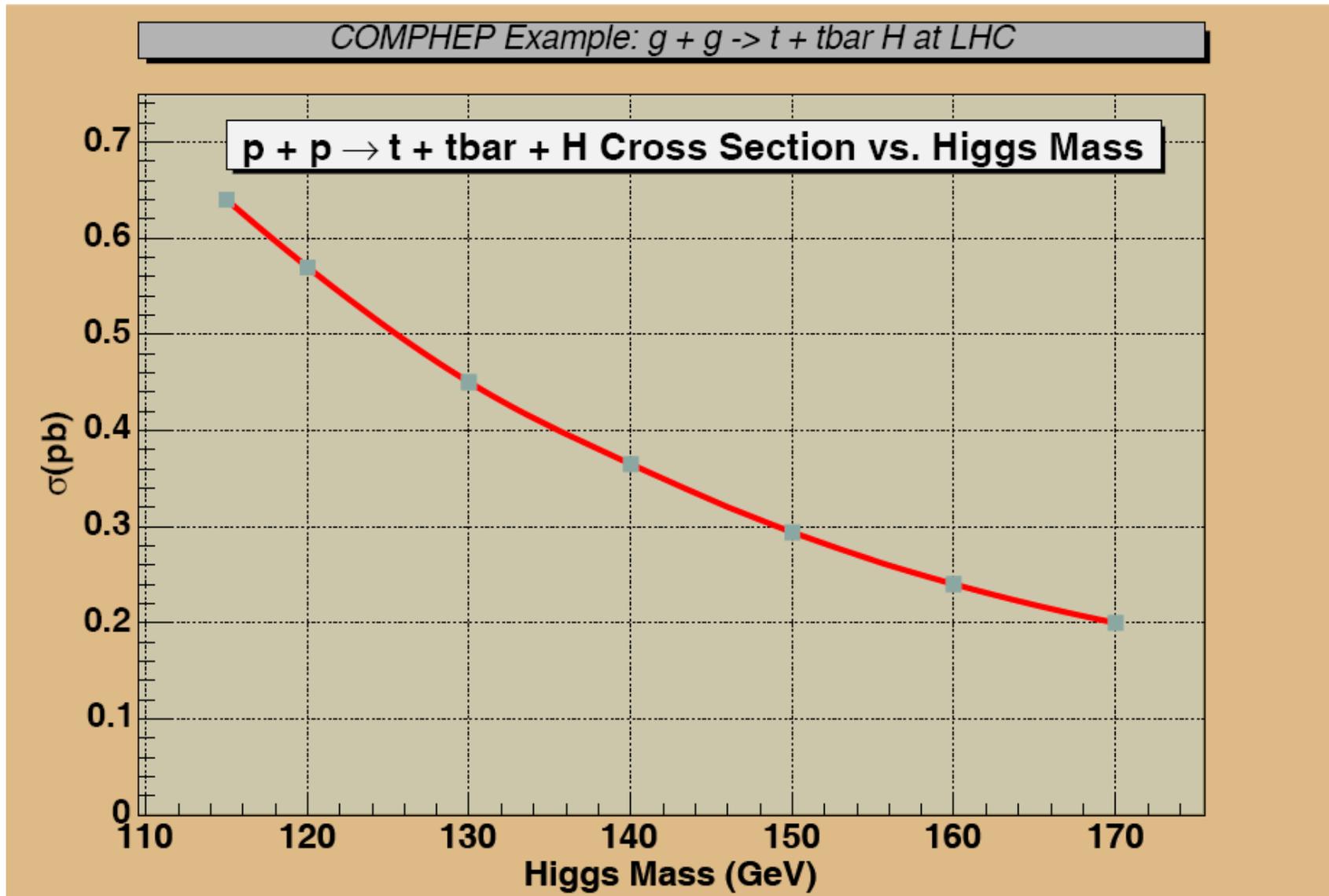
$$p + p \rightarrow t + \bar{t} + H$$

- At the LHC, the mode with best sensitivity for a low-mass Higgs particle appears to be  $H \rightarrow \gamma\gamma$ .
- By looking for the Higgs in association with t quarks, we might be able to see  $H \rightarrow b\bar{b}$ , which would be the dominant decay mode.



(Also have production from initial-state quarks.)

# Signal cross section vs. $m(H)$



$$p + p \rightarrow t + \bar{t} + H$$

$$\sqrt{s} = 14 \text{ TeV} \quad m_H = 115 \text{ GeV}$$

Process	$\sigma$ (pb)
$gg \rightarrow t\bar{t}H$	0.647
$u\bar{u} \rightarrow t\bar{t}H$	0.074
$d\bar{d} \rightarrow t\bar{t}H$	0.045
Total ( $gg+2uu+2dd$ )	0.885

Challenge: Backgrounds  
from  $pp \rightarrow t\bar{t}gg$  and  $pp \rightarrow t\bar{t}b\bar{b}$

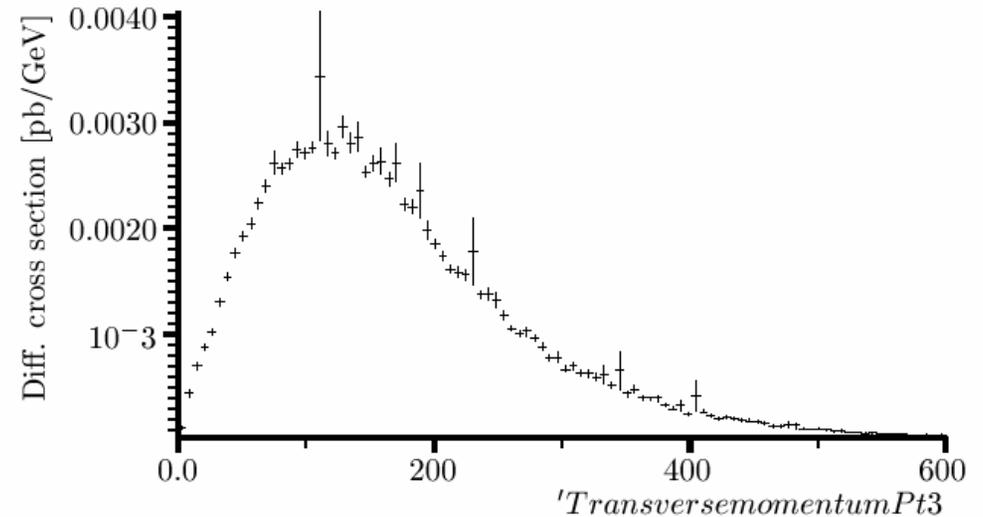
$$\sigma(gg \rightarrow t\bar{t}gg) \approx 400 \text{ pb}$$

$$p_t(g \text{ jets}) > 20 \text{ GeV}, |\eta_{\text{jets}}| < 3, \cos\theta_{jj} < 0.7$$

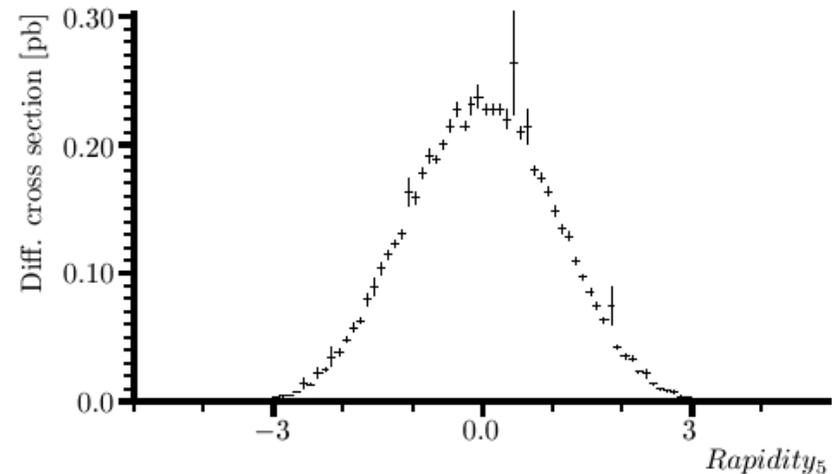
$$\sigma(gg \rightarrow t\bar{t}b\bar{b}) \approx 6 \text{ pb}$$

$$p_t(b \text{ jets}) > 20 \text{ GeV}$$

$G, G- \rightarrow t, T, H$



$G, G- \rightarrow t, T, H$

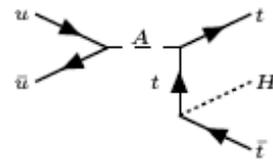
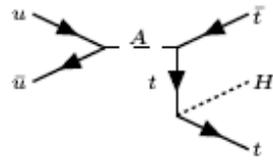
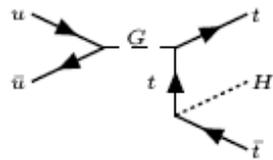
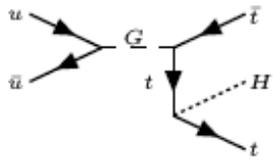


*Background cross sections should not be taken too literally...*

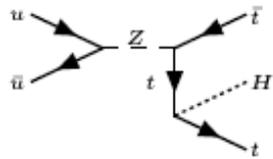
# Conclusions

- CompHEP is very fast and easy. It can provide a quick look at the overall situation for a physics analysis at the LHC.
- It seems to be fairly reliable for electroweak processes.
- Strong interaction processes and corrections are complicated, especially the identification of jets with partons. Predictions based on CompHEP alone—without jet fragmentation— must be treated with a lot of caution!
- Next step: understand how CompHEP events can be given to Pythia to treat the jet fragmentation.

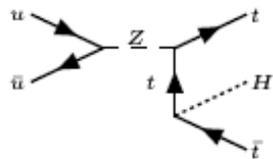
# Extra Slides



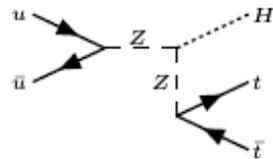
diagr.1



diagr.2



diagr.3

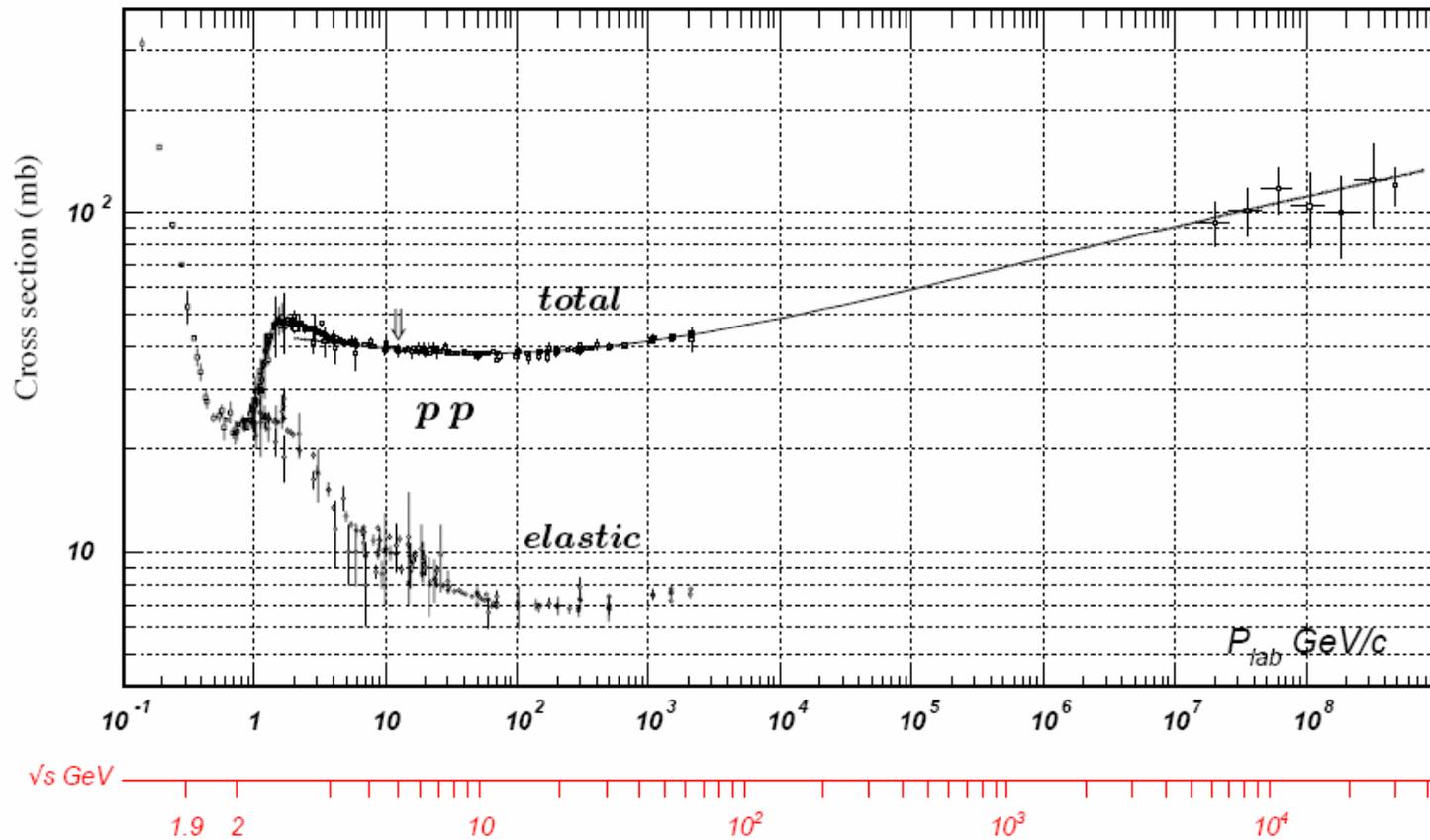


diagr.4

# Energy Scales

- **Band gap of silicon: 1.12 eV**
- **Binding energy of H-atom (n=1): 13.6 eV**
- **Binding energy per nucleon in typical nucleus: 8 MeV**
- **Mass of proton (940 MeV) and neutron (940 MeV)**
- **Mass of b quark: 4.6 GeV**
- **Masses of W (80 GeV) and Z (91 GeV)**
- **Mass of t quark: 174 GeV**
- **Vacuum expectation value of Higgs field**
- **Planck mass:**

# $p+p$ scattering cross section from PDG



# Higgs Branching Fractions

M. Spira Fortsch. Phys. 46 (1998)

