

1. A dumbbell is made of two equal masses,  $m$ , connected by a massless rod of length  $r$ . If  $I_1$  is the moment of inertia with respect to an axis passing through the center of the rod and perpendicular to it and  $I_2$  is the moment of inertia with respect to an axis passing through one of the masses we can say that

(A)  $I_1 = I_2$     (B)  $I_1 < I_2$     (C)  $I_1 > I_2$     (D) needs more info

$$I_1 = m(\frac{1}{2} r)^2 + m(\frac{1}{2} r)^2 = \frac{1}{2} m r^2 \quad I_2 = m r^2 \rightarrow \text{Correct answer is B}$$

2. Consider a solid sphere of radius  $R$  and mass  $M$  rolling without slipping. Which form of kinetic energy is larger, translational ( $K_T$ ) or rotational ( $K_R$ )? (For a sphere rotating around its axis,  $I = \frac{2}{5} MR^2$ )

(A)  $K_R$     (B)  $K_T$     (C) They are equal    (D) Depends on the linear speed

$$K_R = \frac{1}{2} I \omega^2 = \frac{1}{2} (\frac{2}{5} M R^2) (v^2/R^2) = \frac{2}{5} (\frac{1}{2} M v^2) = \frac{2}{5} K_T \rightarrow \text{Correct answer is B}$$

3. Two balls, one of radius  $R$  and mass  $M$ , the other of radius  $2R$  and mass  $8M$ , roll down an incline. They start together from rest at the top. Which one will reach the bottom first? ( $I$  is given in question 2)

(A) The small one    (B) The bigger one    (C) They arrive at the same time

$$\text{Small one: } K_R = \frac{2}{5} (\frac{1}{2} M v^2) \rightarrow K = K_R + K_T = \frac{7}{10} M v^2 \quad \text{But } K = U = Mgh \rightarrow v^2 = \frac{10}{7} gh$$

$$\text{Big one: } K_R = \frac{1}{2} (\frac{2}{5} 8M 4R^2) (v^2/(4R^2)) = \frac{8}{5} M v^2 \rightarrow$$

$$K = K_R + K_T = \frac{8}{5} M v^2 + \frac{1}{2} (8M) v^2 = \frac{28}{5} M v^2$$

$$\text{But } K = U = 8Mgh \rightarrow v^2 = \frac{40}{28} gh = \frac{10}{7} gh \quad (\text{same velocity as small ball})$$

$\rightarrow$  They arrive at the same time  $\rightarrow$  Correct answer is C

4. Two points are on a disk that rotates about an axis perpendicular to the plane of the disk at its center. Point B is 3 times as far from the axis as point A. If the linear speed of point B is  $V$ , the linear speed of point A is:
- (A)  $9V$       (B)  $3V$       (C)  $V$       (D)  $V/3$       (E)  $V/9$

$V = \omega r \rightarrow$  **Correct answer is D**

5. For the two points A and B in the previous question, if the angular speed of point B is  $\omega$ , then the angular speed of point A is:
- (a)  $9\omega$       (b)  $3\omega$       (c)  $\omega$       (d)  $\omega/3$       (e)  $\omega/9$

Angular speed is the same for all points  $\rightarrow$  **Correct answer is C**