MISICS HOMEWORK 7 Griffiths 7.13 = Bocoswt TR $= -emf = -\frac{R^2 T}{4} W B_0 S m \omega t$ = ent Q²TT WBSINWt Griffiths 7.16 Inside: B= MONIZ

 $\overrightarrow{\nabla} \times \overrightarrow{E} = - \frac{\partial \overrightarrow{B}}{\partial E} = - \mu_0 N \frac{dT}{dE}$ In cylindrical coordinates, by symmetry, ceed assuming infinite long solenoid, Ez=0 and $\overline{E} = \overline{E}_{p}(r) \dot{\phi} + \overline{E}_{r}(r) \dot{f}$ But $E_r(r)$ must be = 0by considering the flex through the red spherical surface shown below because no charge enclosed



Outside Soleword, B=0, therefore the some algebra leads to $\partial(FE) = 0$ which means that FE= Constant Or E= Constant insure continuity of T=Q 10 $E = \frac{\mu_0 N q^2}{2\Gamma} \frac{JT}{Jt} \frac{m}{direction}$ Outside solenoid, r>a Another way of doing this



this then ellows you to solve for E_ Griffiths 7.25 B=MonI Flux through one turn is Q=BTTR'= MONTRZI There are al turns in a length d of solenoid So the total flux for a length $lin \phi = \mu_0 n^2 T R^2 e T$ If L is the self-inductive then \$=LI_Turs

 $L = M_0 M^2 \pi R^2 per unit length$ Gniffiths T.28 $\begin{array}{c|c}
Q & + & L & d^2 \\
\hline
C & & d^{22} \\
\hline
C & & d^{22}
\end{array}$ $\frac{d^2 Q}{dt} = -\frac{1}{LC} Q$ This is the some eqtin of hormonic motion_ Undomped oscilletor $Q(t) = l_0 cos(wt + 5) w = 1$ the t=0 condition goves

 $\delta = 0$ and $Q_{0} = CV$ $T(t) = \frac{dQ}{dt} = \frac{T(t)}{t} = -wCVsinwt$ with a Resistor, the differential lquotion becomes $L \frac{d^2Q}{dt} = \frac{R}{R} \frac{Q}{dt} + \frac{Q}{C} = 0$ This is the equation for a deciped hormonic oscilletor which I pope you have plready seen in methonics clos (!)



Since the velocity is in the y direction we should switch to contestion coordinates Bz MOJ (- YX+XJ) ZT F F F F) $B = \frac{M \circ I/2N}{X^2 + y^2} \left(-y x + x y\right)$ here x end y ore measured from the wire. Since the wire is traveling to the right with velocity of I should replace y with y-ot in the fixed coordinete system $B = \frac{M \circ J/2\pi}{\chi^2 + (y - v +)^2} \left(\frac{(y - v +)\chi + \chi \hat{y}}{\chi^2 + (y - v +)^2} \right)$

Now I use $\nabla x \vec{E} = -\frac{\partial \vec{B}}{\partial t}$ $\frac{\partial \hat{B}}{\partial t} = \frac{M \sigma I / 2\pi}{(X + (y - \sigma t)^2) X} \left[\frac{\partial \nabla (X + (y - \sigma t)^2) X}{(X + (y - \sigma t)^2) I} \right] \left[\frac{\partial \nabla (X + (y - \sigma t)^2) X}{(y - \sigma t) I} \right] \left[\frac{\partial \nabla (X + (y - \sigma t)^2) X}{(y - \sigma t) I} \right] \left[\frac{\partial \nabla (X + (y - \sigma t)^2) X}{(y - \sigma t) I} \right] \left[\frac{\partial \nabla (X + (y - \sigma t)^2) X}{(y - \sigma t) I} \right]$ At t=0 $\frac{\partial B}{\partial B} = \frac{M \circ T/2T}{2T} \left[\sqrt{(\chi^2 + \gamma^2)} + \right]$ $\frac{\partial t}{(\chi^2 + \gamma^2)^2} \left[2\sigma \chi g \dot{g} - 2\sigma g \dot{\chi} \right]$ $\frac{\partial B}{\partial t} = \frac{\mu_0 F/2\pi}{(x^2 + y^2)^2} \nabla \left[(x^2 - y^2) \hat{x} + 2x \hat{y} \hat{y} \right]$ $\frac{\partial F}{\partial t} = \frac{\mu_0 F/2\pi}{(x^2 + y^2)^2} \nabla \left[(x^2 - y^2) \hat{x} + 2x \hat{y} \hat{y} \right]$ At this point we should more boek to cylindrical coordinates because at t=0 we have cylindrical symmetry

 $\frac{1}{X} = \frac{1}{F}\cos\phi - \sin\phi\phi$ Bquetions Y = r smp + cosop Los Griffiths So the quentity in squere brockets becomes $\Gamma^{2}\left[\left(\cos^{2}\phi - \sin\phi\right)\left(\cos\phi\hat{r} - \sin\phi\hat{\phi}\right)\right]$ $+2\sin\phi\cos\phi\left[\sin\phi\hat{F}+\cos\phi\hat{\phi}\right]$ $= r^2 \left(\cos \phi - \cos \phi \sin \phi + 2 \sin \phi \cos \phi \right) \hat{r}$ $+(sin^{3}\phi-sin\phi\cos^{2}\phi+2sin\phi\cos\phi)\phi$ $= \Gamma^{2} \left[\cos \phi \left[\cos \phi + \sin \phi \right] \right] + t$ SINQ [SINQ + cosq)] $= f^2 (\cos \phi f + \sin \phi \phi)$

Plugging this into the equation for <u>dB</u> I get $\frac{\partial B}{\partial t} = \frac{M \partial I v}{2\pi r^2} \left[\cos \phi \hat{r} + \sin \phi \phi \right]$ Now I have to find E such Hot VXE = DB oerd TE = OB oerd VE = O I note that E count depend on Z by symmetry _ Also, the needs to go to zero os r->00

 $\vec{E}(r,\phi) = \vec{E}_{\Gamma}(\Gamma,\phi)\vec{F} + \vec{E}_{\phi}(\Gamma,\phi)\vec{\phi}$ $+E_7(r,\phi)^2$ $\overrightarrow{\nabla}, \overrightarrow{E} = 0 \implies \frac{1}{r} \frac{\partial}{\partial r} (r \overrightarrow{E}_r) + \frac{1}{r} \frac{\partial \overrightarrow{E}_0}{\partial \phi} = 0$ $\left(\overrightarrow{\nabla} \times \overrightarrow{E}\right)_{r} = \frac{1}{r} \frac{\partial \overrightarrow{E}_{2}}{\partial \phi} = -\frac{\mu_{\theta} I v}{2\pi r^{2}} \cos(2)$ $\left(\overline{\nabla}\times\overline{E}\right)_{\Phi} = -\frac{\partial\overline{E}_{2}}{\partial\Gamma} = -\frac{\mu_{0}\overline{L}\nu}{2\pi\Gamma^{2}}\sin\Phi$ (3) $\left(\nabla x E\right)_{2} = \frac{1}{r} \left[\frac{\partial}{\partial r} \left(r E_{p} \right) - \frac{\partial E_{r}}{\partial \phi} \right] = 0$ 4) The 3rd equation gives $E_{Z} = -\frac{\mu_{o} I v}{2\pi r} sin\phi$

But since we went E-10 es $\Gamma \rightarrow \infty$, $f(\phi) = constant = 0$ So $E_2 = -\frac{\mu_0 Tv}{2\pi t} Sin \phi$ This solution also satisfies eath 2 Equations (1) and (4) are satisfied $H = E_{p} = 0$ PROBLEN 7 Energy slored = $E = \frac{1}{2\mu_0} \frac{B^2}{AL} \frac{A = -\frac{1}{4} T d^2}{4}$ $E = \frac{1}{8} \frac{B^2 \pi J^2}{M_0}$

 $E = \frac{1}{8} + \frac{1}{4107} (3.8)^2 + 6^2 + 13 \text{ Soules} = 2.1 + 6^9 \text{ J}$ 0 41 M USING https://calculator.academy/joules-to-tnt-calculator/ Huis corresponds to the equivelent of 0.5 tons of ThT