

GRIFFITHS 10.4

 $\vec{E} = -\vec{\nabla}V - \partial\vec{A}$ E'= Aow Cos(kx-wt) j $\vec{B} = \vec{\nabla} \times \vec{A}$ B=Aok cos(kx-wt)Z This is simply a place wave solutions which we know "works" provided w/R=c/ It is a weve propagating in the & direction. The orientetion of the frelds in such e were must be B in the direction of RXE Since $\hat{x} \times \hat{y} = \hat{z}$, the orientations are elso OK GRIFFITHS 10.6 AV: original potentiels A'V: genze transformed potentiels

 $\vec{A} = \vec{A} + \vec{\nabla} \vec{\lambda} \quad \vec{V} = \vec{V} - \vec{J} \vec{\lambda}$ Wout $\overline{\nabla}A = -M_0 \varepsilon_0 \partial V' - Con I find \lambda$ $\nabla \left(\overrightarrow{A} + \overrightarrow{V} \overrightarrow{\lambda} \right) = -\mu_0 \varepsilon_0 \frac{\partial V}{\partial t} + \mu_0 \varepsilon_0 \frac{\partial^2 \overrightarrow{A}}{\partial t^2}$ $-\left[\overline{\nabla} \overline{A}^{'} + Mo \varepsilon_{0} \frac{\partial V}{\partial t}\right] = \overline{D}^{2} \lambda$ Cell this $f(\vec{r},t)$ $\Delta = f(\vec{r},t)$ This is like 10.16 (e) which we know how to solve We can always pick V=0 by choosing $\lambda(t) = (Vdt)$ We connot alweys pick A=0 because that would mean B=curl A=0

GRIFFITHS 10.8 Equation 10.19 $\frac{d\tilde{A}}{dt} = \frac{\partial A}{\partial t} + (\vec{V} \cdot \vec{V}) \vec{A}' = (\vec{V} \cdot \vec{V}) \vec{A}'$ $\frac{dA}{dt} = \frac{1}{2} \left[\left(\vec{V} \cdot \vec{\nabla} \right) \left(\vec{\Gamma} \times \vec{B} \right) \right]$ $= -\frac{1}{2} \left[\left(V_{X} \frac{\partial}{\partial x} + V_{y} \frac{\partial}{\partial y} + V_{z} \frac{\partial}{\partial z} \right) \right] \left(y B_{z} - z B_{y} \right) \hat{x} + \left(z B_{X} - x B_{z} \right) \hat{y} + \left(z B_{X} - x B$ (×By-yBs) Z] $= -\frac{1}{2} \left[V_{x} \left[-B_{z} \hat{y} + B_{y} \hat{z} \right] + V_{y} \left[B_{z} \hat{x} - B_{x} \hat{z} \right] \right]$ $+V_{z}\left[-B_{y}\hat{x}+B_{x}\hat{y}\right]$ $= -\frac{1}{2} \left[\left(V_y B_z - V_z B_y \right) X + \left(-V_x B_z + B_x V_x \right) \right] \right]$ continued

 $+ \hat{z} (V_X B_Y - V_Y B_X)$ $\frac{dA}{JL} = -\frac{1}{Z} \left(\overrightarrow{V} \times \overrightarrow{B} \right)$ Equation 10,20 $d\left(\vec{p}+q\vec{A}\right) = -q\vec{V}\left(V-\vec{v}\cdot\vec{A}\right)$ The LHS in $\frac{d\vec{p}}{dt} + q \frac{d\vec{A}}{dt} = \frac{d\vec{p}}{dt} - \frac{q}{2} \left(\vec{V} \times \vec{B} \right)$ The RHS is $-q\vec{\nabla}V - \frac{1}{2}q\vec{\nabla}(\vec{v}\cdot(\vec{r}\times\hat{B})) =$ $q\vec{E} - \frac{1}{2}q\vec{\nabla}(\vec{v}\cdot(\vec{F}\times\vec{B}))$ LI Wrote E= -90V.... magnetostetic & electrostetic

Consider the second term in the RHS $\nabla \left(\overline{\sigma} \cdot \left(\overline{r} \times \overline{B} \right) \right) = \nabla \left(\overline{r} \cdot \left(\overline{B} \times \overline{\sigma} \right) \right)$ using $\vec{R} \cdot (\vec{b} \times \vec{c}) = \vec{b} \cdot (\vec{c} \times \vec{o})$ But for any vector $\vec{\nabla}(\vec{F} \cdot \vec{a}) = \vec{\nabla} (\boldsymbol{\Sigma} \cdot \vec{a}) = \vec{Q}$ -) This is then BXV SO RHS IS $\cdot \qquad q\vec{E} - q(\vec{B}\times\vec{V}) = q\vec{E} + q(\vec{V}\times\vec{B})$ Setting LHS=RHS we have $\frac{d\vec{p}}{dt} = \frac{q}{z}(\vec{v}\times\vec{B}) = q\vec{E} + \frac{q}{z}(\vec{v}\times\vec{B})$ $\frac{dP}{dt} = q\left(\overline{E} + (\overline{V}_X \overline{B})\right)$