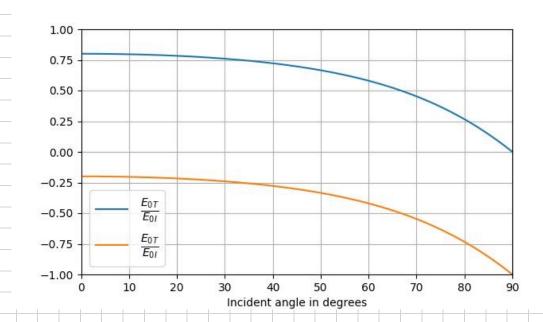
PHYSICS 110 B HOMEWORK 4 GRIFFITHS 9,16 Aeiex + Beibx = Ceicx Set x=0 A+B=C Multiply by e-iex A+Bei(b-e)x - Cei(c-e)x (1) Take imaginary nort of (1) $B \sin(b-\alpha) \times = C \sin(c-\alpha) \times$ Clearly this works if e=b=c. Now exame that this is not true and see if we can get to a contraddiction (when e, b, c are non-zero) If b te I can set x = II which gives 0 = C sin C-12 TI b-a For C = 0, I must have C-R = N where N=integer Similarly if the I can set x = I which gives B sin b-1277 = 0 For B = 0, I must have 5-e = M where M = integer The only way that the two circled equations can work in V=M=1This means b-a=c-a which gives b=c

So I can still have in principle b=c+a Equation (1) then becomes (setting c=b) A + B & (b-a) x = (e (b-a) x A e = C-B The imaginary port in Asin(2-5)x = 0 In order for this to work et ell values of x, I must have that R=b and since b=c, R=b=c CONTRADDICTION REACHED GRIFFITHS 9.17 Will use the sketch from Figure 9.14 in Griffiths And write the k vectors according http://hep.ucsb.edu/people/claudio/ ph110b-f24/GriffithClarification2.pdf $\hat{k}_I = \sin \theta_I \hat{x} + \cos \theta_I \hat{z}$ $k_R = \sin \theta_R \hat{x} - \cos \theta_R \hat{z}$ $\hat{k}_T = \sin \theta_T \hat{x} + \cos \theta_T \hat{z}$

Dropping the elikit wit terms, on the surface we have
$$\vec{E}_{3} = \vec{E}_{92} \hat{y} \quad \vec{B}_{3} = \frac{1}{V_{1}} (\hat{k}_{1} \times \hat{E}_{3}) = \frac{E_{07}}{V_{1}} \left[\frac{1}{0} \hat{x} + \frac{1}{2} \hat{x} + \frac{1}$$

Using d= OSOT B= MINTS COSOT B= MINTS Eos-EoR = &BEOS The sum of the two circled equetions gives $2E_{0T} = (\alpha \beta + 1)E_{0T}$ $E_{0T} = \frac{2}{\alpha \beta + 1}E_{0T}$ Substituting into the 1st circled equation $E_{0J} + E_{0R} = \frac{2}{\alpha_{\beta+1}} E_{0J} = \frac{1-\alpha_{\beta}}{\alpha_{\beta+1}} E_{0J} = \frac{1-\alpha_{\beta}}{1+\alpha_{\beta}} E_{0J}$ For the required Sketch, we need XB_ We are also going to use M = M2 Equation 9.111 in Griffiths $\alpha \beta = \beta \sqrt{1 - \sin^2 \theta_5} / \beta^2 - \sqrt{\beta^2 - \sin^2 \theta_5}$ $\cos \theta_1 \cos \theta_2$ Here then are the plots as requested (on the next page)



For a Brewster angle we want
$$Eo_R = 0$$
 which means $\alpha \beta = 1$ We had $\alpha \beta = \sqrt{\beta^2 - \sin^2 \theta_x}$ which means $\cos \theta_I = \sqrt{\beta^2 - \sin^2 \theta_x}$

This only works if $\beta = 1$, ie if the two medie have the same properties (optically in distinguishable)

At normal incidence
$$\alpha\beta = \beta$$

For the reflection and transmission coefficient we use equations 9.116 and 9.117 $R = \left(\frac{E_{OR}^{2}}{E_{OI}}\right) \qquad R = \left(\frac{1 - \alpha \beta}{1 + \alpha \beta}\right)^{2}$ $T = \alpha \beta \left(\frac{E_{o+}}{E_{o}}\right)^2 = 4\alpha \beta \left(\frac{E_{o+1}}{E_{o}}\right)^2$ $R + T = \frac{1 + \alpha \beta^2 - 2\alpha \beta + 4\alpha \beta}{\left(1 + \alpha \beta\right)^2}$ GRIFFITHS 9.21 (a) Eq 9.128 $K = \omega \sqrt{\frac{\varepsilon}{2}} \left[\sqrt{1 + \left(\frac{\varepsilon}{\varepsilon}\right)^2} - 1 \right]^{\frac{1}{2}}$ For $\sigma < \langle \varepsilon \omega \rangle / 1 + \langle \sigma \rangle \sim 1 + \frac{1}{2} \langle \varepsilon \omega \rangle^2$ Thus $k = \omega \left[\frac{\varepsilon}{2} \mu \right] \left[\frac{1}{2} \left(\frac{\sigma}{\varepsilon} \omega \right)^2 \right] = \frac{\omega}{2} \sqrt{\varepsilon} \mu \frac{\sigma}{\varepsilon} \omega$ K= = TM d= = = Z FE For H20 E= 80 Es (From Wikipedia, et 20°C)

M = Mo (not magnetic)

T = 5.5 10 5 (From google search,)

with pure water

$$d = \frac{2}{5.5 \cdot 10^{-12}} \sqrt{\frac{80.9 \cdot 10^{-12}}{4\pi \cdot 10^{-7}}} = 3.6 \cdot 10^{5} \sqrt{5.7 \cdot 10^{-4}}$$

$$d \approx 28 \text{ Km}$$

$$0 \approx 28 \text{ Km}$$

$$9.128 \text{ we see that } k \approx k$$

$$So \ d = \frac{1}{k} \text{ end since } k \approx 2\pi \text{ d} = \frac{\lambda}{2\pi}$$

$$In \text{ terms of } \omega, \varepsilon, \text{ etc} \Rightarrow k$$

$$k \approx \omega \sqrt{\frac{\varepsilon}{2}} \left[\sqrt{\frac{\varepsilon}{\varepsilon}} \sqrt{\frac{\varepsilon}{\varepsilon}} \right]^{2} + \sqrt{\frac{\varepsilon}{2}} \sqrt{$$

Equation 9.139 in the limit
$$\frac{1}{E}$$
 >>1

Bo $\frac{1}{E}$ | $\frac{1}{E$