## Physics 110B, Discussion Session 5

The optical length of the path traversed by a light ray traveling betteen the points P and Q is defined by the line integral along the path

$$L = \int_P^Q n d\ell$$

where n is the index of refraction along the path.

Fermat's principle states that the actual path length is the one such that L is an extreme (usually a minimum). If n is constant, the path that minimizes L is a straight line. Note that minimizes the optical path also correspond to minimizing the time taken to go from P to Q.

Let the xy plane be the boundary between two dielectrics, index of refraction  $n_1$  for z < 0,  $n_2$  for z > 0. Let P and Q have coordinates  $(x_1, y_1, z_1)$  and  $(x_2, y_2, z_2)$  with  $z_1 < 0$ . and  $z_2 > 0$ . The (PQ) path will cross the z plane at some point (x, y, z = 0).

Show that according to Fermat's principle

- 1. The path will lie in a plane (the plane of incidence)
- 2. Snell's law is satisfied.

Hint: we no loss of generality you can shoose the axes such that  $y_1 = y_2 = 0$ .