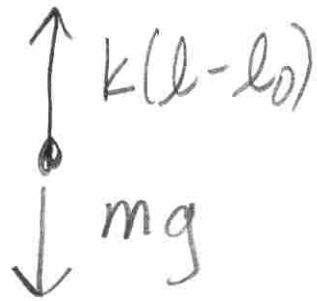


$$l - l_0 = 0.4 \text{ meters}$$

Period for small oscillations is:

- (A) Not enough information
- (B) 5 s
- (C)  $2\pi$  s
- (D)  $\frac{2\pi}{5}$  s
- (E)  $\frac{\pi}{5}$  s



$$k(l-l_0) = mg$$

$$k = \frac{mg}{l-l_0}$$

$$\omega = \sqrt{\frac{k}{m}} = \sqrt{\frac{mg}{m(l-l_0)}}$$

$$T = \frac{2\pi}{\omega} = 2\pi \sqrt{\frac{(l-l_0)}{g}}$$

$$= 2\pi \sqrt{\frac{0.4}{10}}$$

$$= 2\pi \sqrt{0.04} = 0.2 \cdot 2\pi$$

$$T = 0.4\pi = \frac{2\pi}{5} \text{ s}$$

$$y(0) = 0$$

$$\dot{y}(0) = -2 \text{ m/s}$$

$$y(t) = A \sin(\omega t) + B \cos(\omega t)$$

$$y(0) = B = 0$$

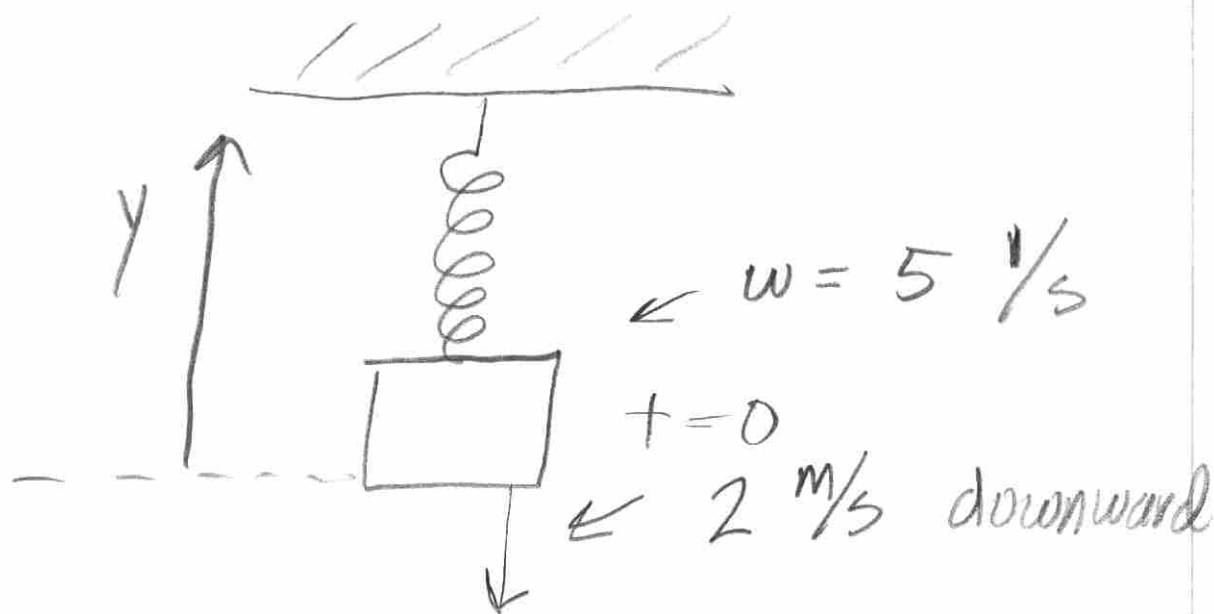
$$\dot{y}(t) = \omega A \cos(\omega t) - \omega B \sin(\omega t)$$

$$\dot{y}(0) = \omega A = -2 \text{ m/s}$$

$$A = -\frac{2}{\omega} = -\frac{2 \text{ m/s}}{5 \text{ 1/s}}$$

$$A = -0.4 \text{ m}$$

$$y(t) = -0.4 \sin(5t)$$



$$y(t) =$$

- (A)  $2 \cos(5t)$  meters
- (B)  $-2 \cos(5t)$  "
- (C)  $-0.4 \sin(5t)$  "
- (D)  $-2 \sin(5t)$  "
- (E)  $-0.4 \cos(5t)$  .

# Momentum

Chapter 3 K&K  
a RHK4  
(no energy)

$$\vec{F}_{Net} = m \vec{a} = m \dot{\vec{v}}$$

hidden assumption:  $m = \text{constant}$   
(relativity, the kilogram)  
more generally,

$$\vec{F}_{Net} = \frac{d}{dt} (m \vec{v})$$

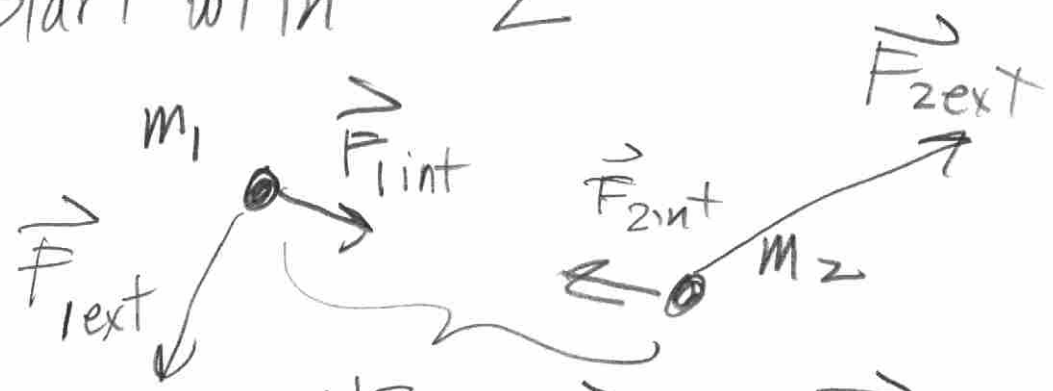
the momentum

$$\vec{p} = m \vec{v}$$

Curious situation: system of particles...

Every ball, block, etc.  $\approx 10^{24}$  atoms!

Start with 2



1/3:  $\vec{F}_{1int} = -\vec{F}_{2int}$

$$\vec{F}_{1\text{net}} = \vec{F}_{1\text{ext}} + \vec{F}_{1\text{int}} = \frac{d}{dt} (\vec{p}_1)$$

$$\vec{F}_{2\text{net}} = \vec{F}_{2\text{ext}} + \vec{F}_{2\text{int}} = \frac{d}{dt} (\vec{p}_2)$$

cancel

$$\vec{F}_{1\text{ext}} + \vec{F}_{2\text{ext}} = \frac{d}{dt} (\vec{p}_1 + \vec{p}_2)$$

total momentum

independent of: internal forces

$$M \vec{R} = \frac{d}{dt} (\vec{p}_1 + \vec{p}_2)$$

$(m_1 + m_2)$  (to be found)  $\frac{dm_1}{dt} = 0, \frac{dm_2}{dt} = 0$

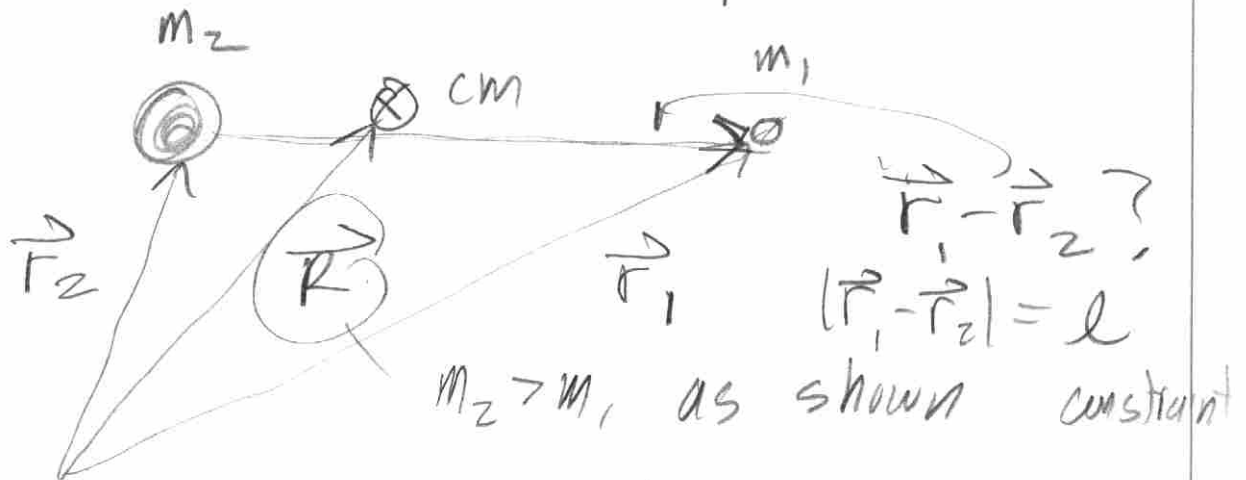
$$= m_1 \vec{v}_1 + m_2 \vec{v}_2$$

$$\vec{R} = \frac{m_1 \vec{v}_1 + m_2 \vec{v}_2}{m_1 + m_2}$$

$$\vec{R} = \frac{m_1 \vec{r}_1 + m_2 \vec{r}_2}{m_1 + m_2}$$

$\vec{R}$  is called center of mass

Dumb-bell: balance point.



$$\vec{R} = \frac{m_1 \vec{r}_1 + m_2 \vec{r}_2}{m_1 + m_2}$$

$$f_1 = \frac{m_1}{m_1 + m_2}$$

$$f_2 = \frac{m_2}{m_1 + m_2}$$

$$\vec{R} = f_1 \vec{r}_1 + f_2 \vec{r}_2 \quad 0 \leq f \leq 1$$

$$m_2 = 0, \quad f_1 = 1, \quad f_2 = 0$$

$$\vec{R} = \vec{r}_1$$

$$m_1 = 0, \quad f_1 = 0, \quad f_2 = 1$$

$$\vec{R} = \vec{r}_2$$

LINEAR between these two limits.